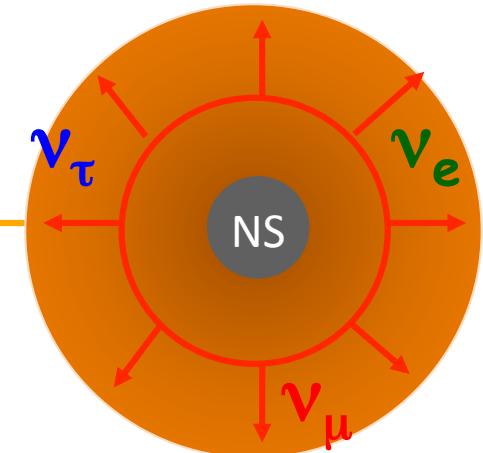


# *Neutrinos* and Supernovae

**v**



**Cristina VOLPE**  
(Institut de Physique Nucléaire Orsay, France)



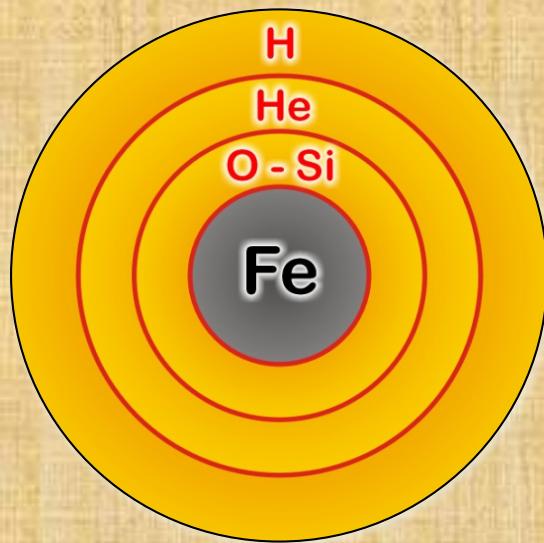
# OUTLINE

## ★ Introduction

★ **Neutrino flavour conversion  
in explosive media**

★ **Observations : learning  
about supernova dynamics  
and neutrino properties**

# Core-collapse supernovae (SN)



- Stars with masses :  
 $6 \text{ Msun} < M < 8 \text{ Msun}$  O-Ne-Mg SN  
 $M > 8 \text{ Msun}$  Iron-core SN
- 99 % of the gravitational energy ( $10^{53}$  ergs) is radiated as neutrinos and anti-neutrinos of all flavours.
- The burst lasts about 10 seconds.
- The SN neutrino fluxes span the energy range from a few to 50 MeV (with a tail).

# Why investigating SN neutrinos?



## SN dynamics

- explosion mechanism not unravelled yet
- nucleosynthesis processes  
(r-process, vp-process, v-process)
- to test SN models
- flavour conversion phenomena in explosive environments

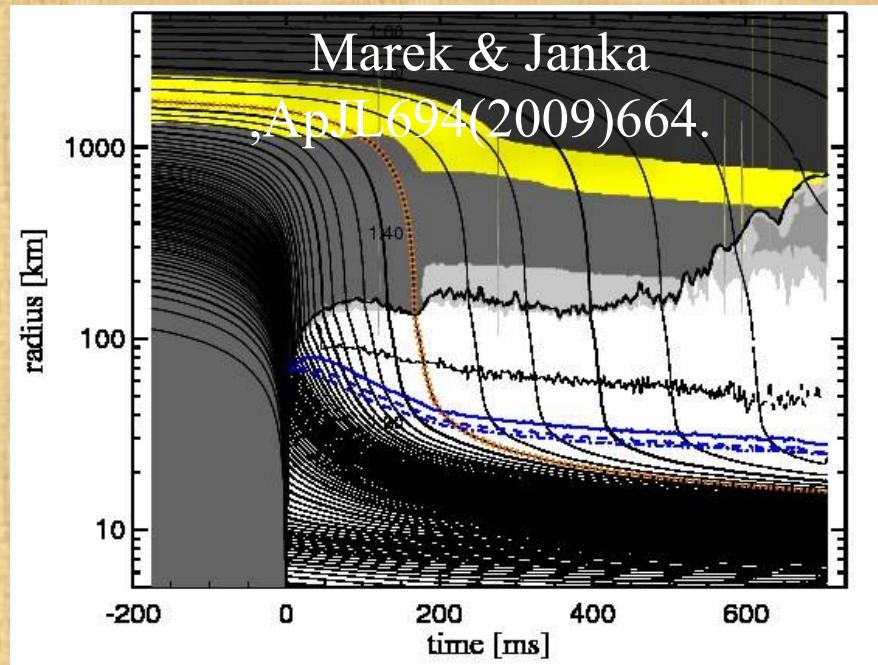


## v properties

- unknown neutrino properties impact SN physics, e.g.  
 $\theta_{13}$ , mass hierarchy, sterile neutrinos, non-standard interactions, leptonic CP violation ( $\delta$ ), ...

# Do iron-core SNe explode ?

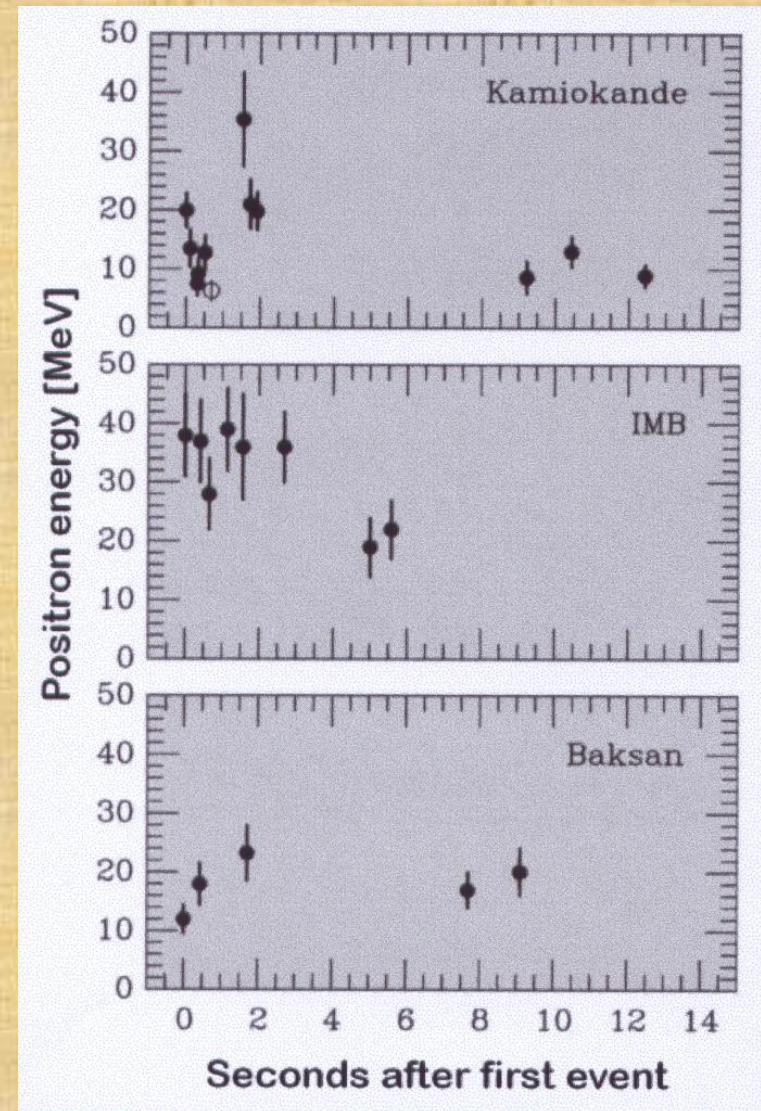
- A longstanding problem.
- In the last decade, SN simulations have become 2D-3D, include convection and realistic neutrino transport.



The explosion mechanism delineated :  
a combination of  
convection- neutrino - hydro  
instability (SASI).

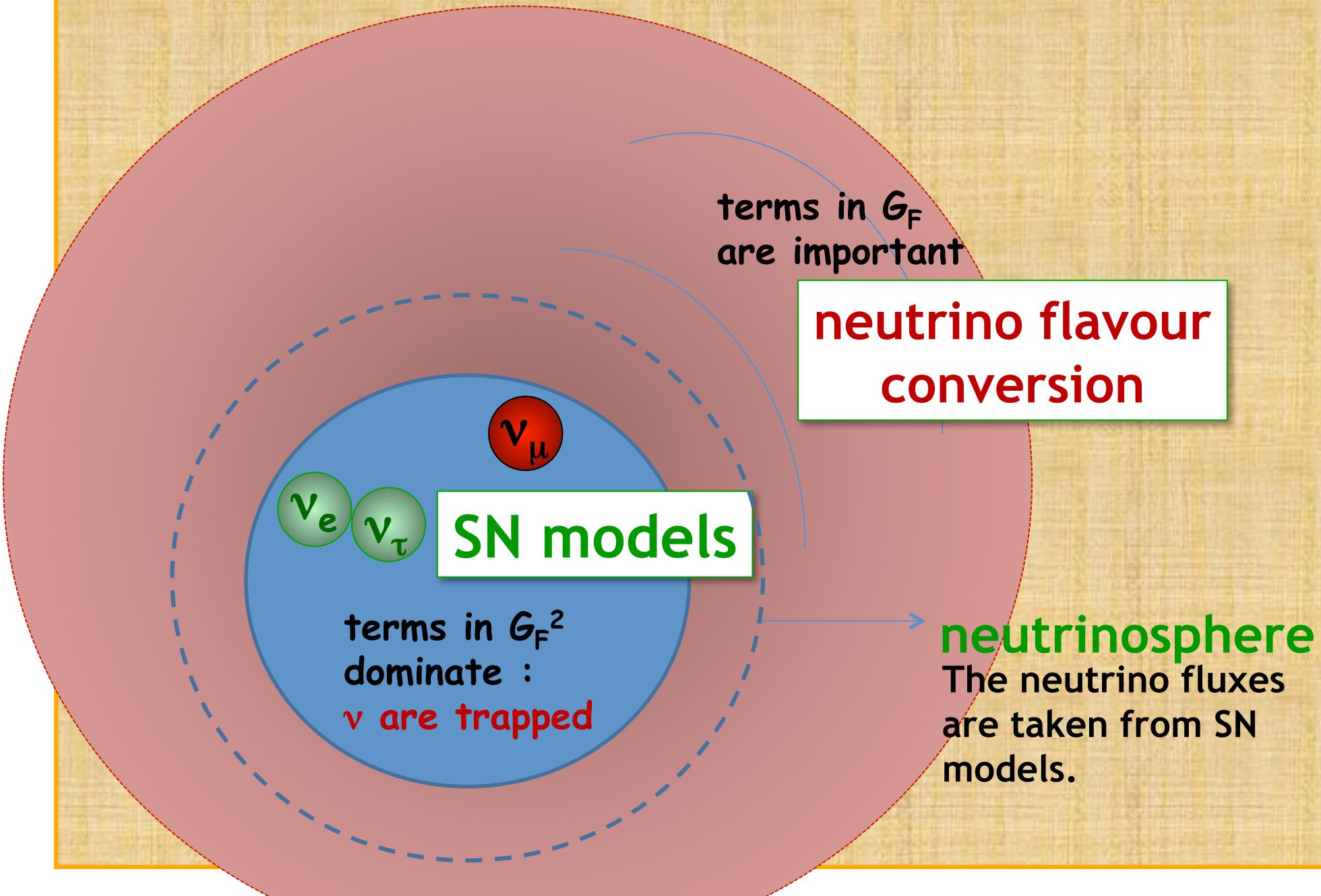
# SN1987A events

SN1987A LMC (50 kpc)

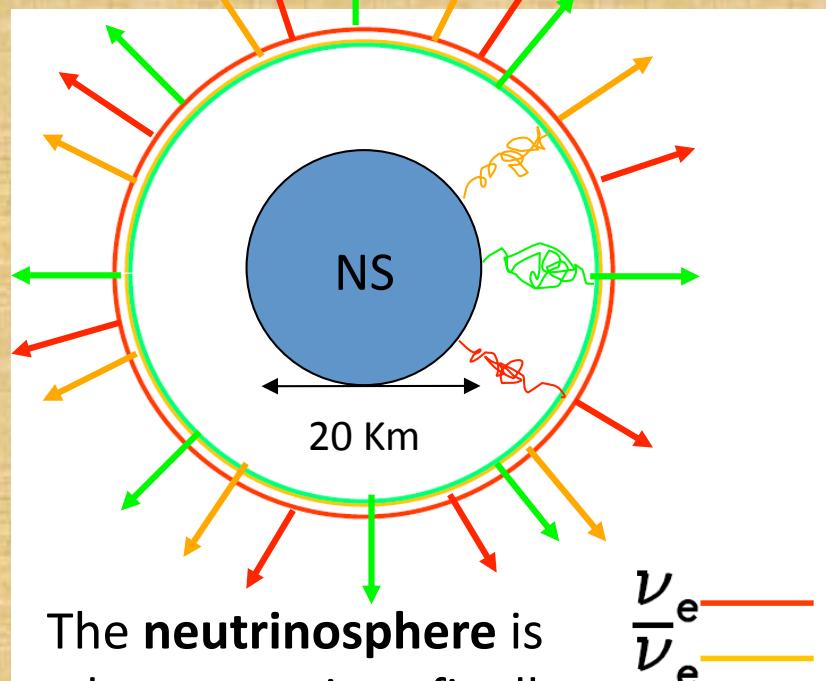


Expectations are roughly confirmed.

# A comment on the models

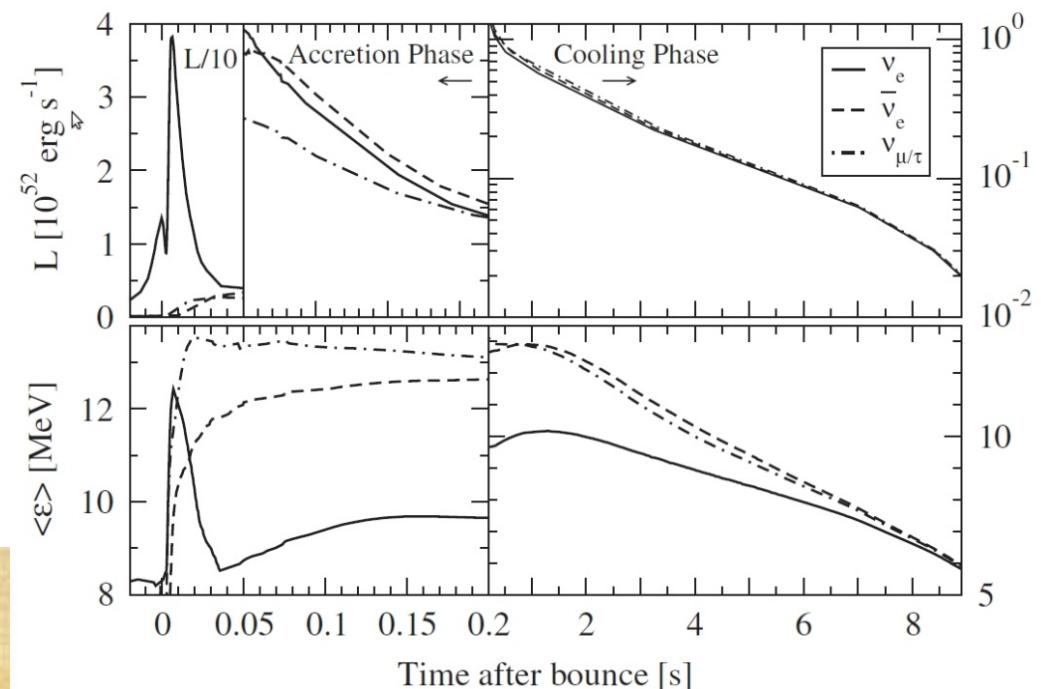


# At the neutrinosphere : the $\nu$ fluxes



Different neutrino flavours have different neutrinospheres. Muon and tau neutrinos only have NC while electron (anti)neutrinos undergo NC and CC.

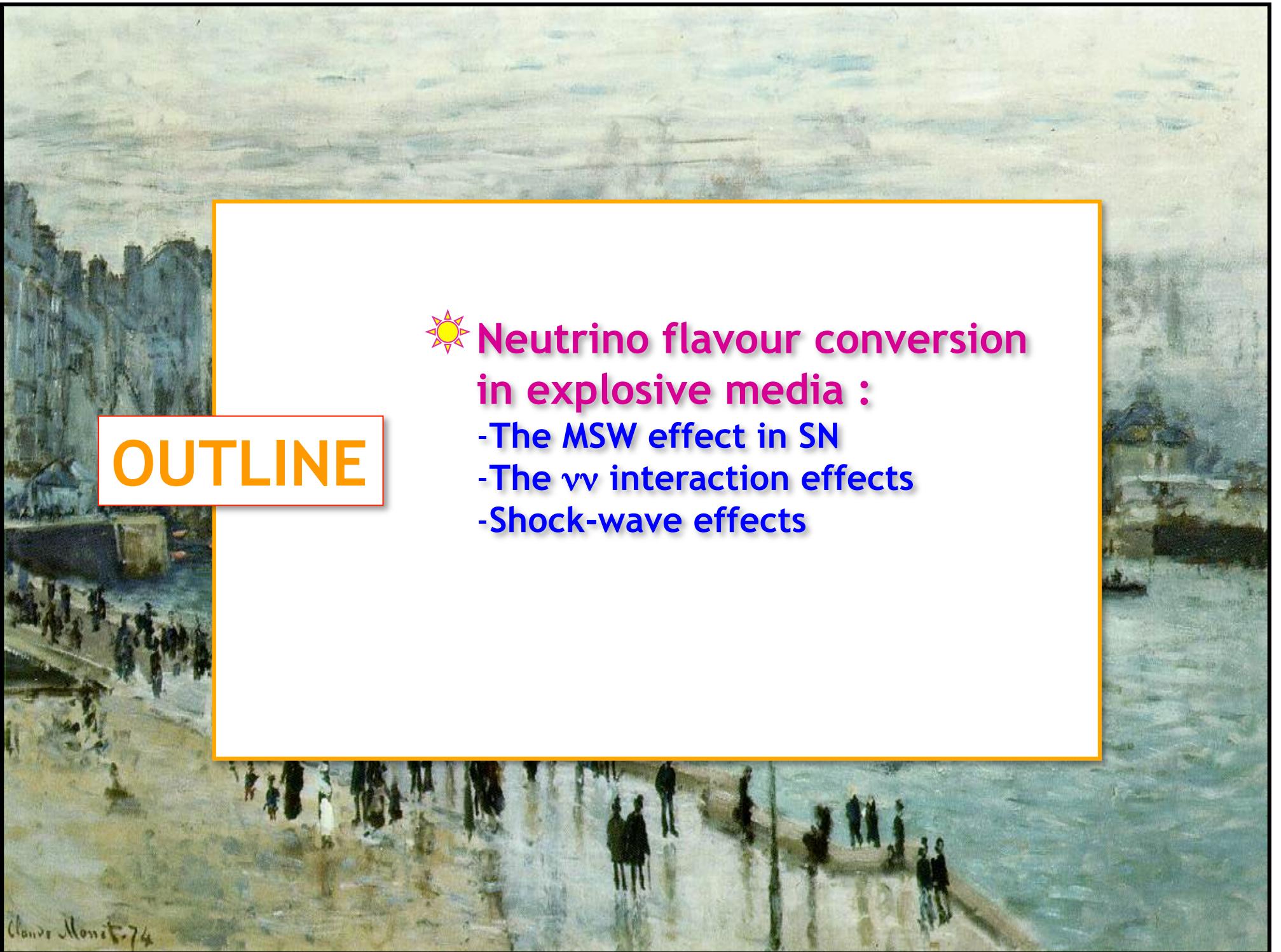
$$\langle E_{\nu e} \rangle < \langle E_{\bar{\nu} e} \rangle < \langle E_{\nu x} \rangle$$



Neutrinos follow closely the explosion.

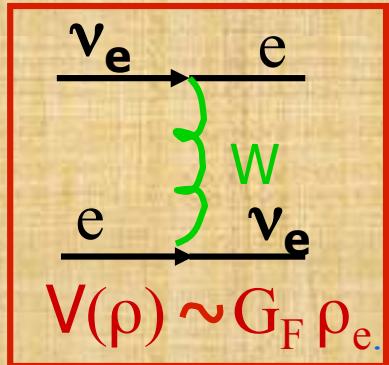
# OUTLINE

☀ Neutrino flavour conversion  
in explosive media :  
-The MSW effect in SN  
-The  $\nu\nu$  interaction effects  
-Shock-wave effects



# Neutrino flavour conversion in matter

## The Mikheev-Smirnov-Wolfenstein (MSW) effect



Neutrino coupling with matter induces a resonant flavour conversion.

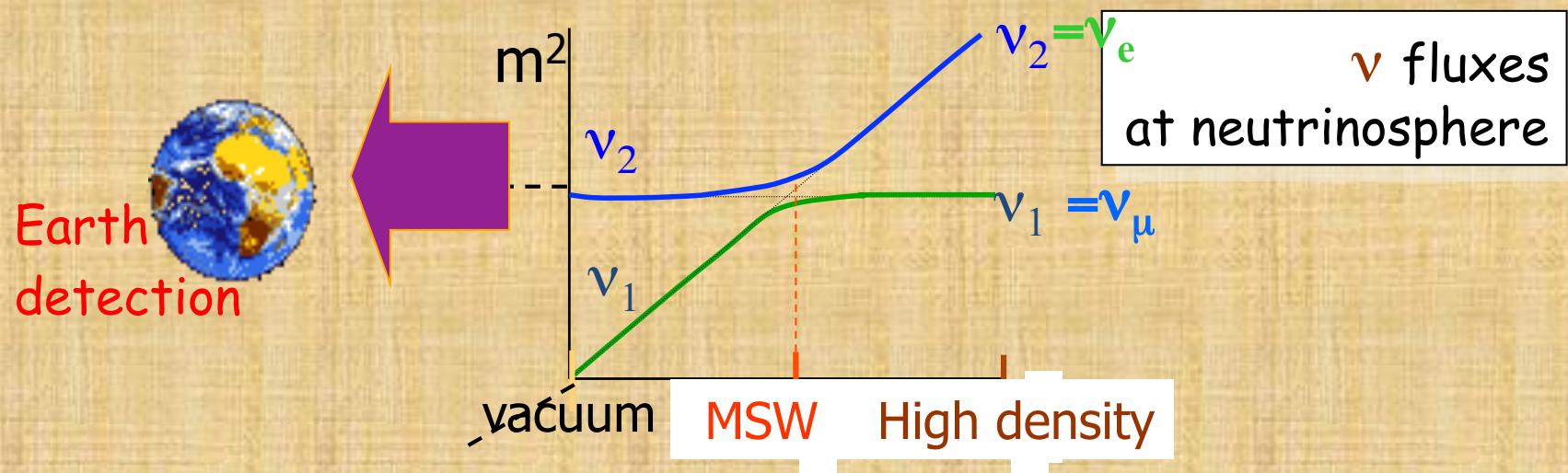
In the flavour basis, the neutrino evolution equations in matter :

$$i \frac{\partial}{\partial t} \begin{pmatrix} \Psi_e \\ \tilde{\Psi}_\mu \\ \tilde{\Psi}_\tau \end{pmatrix} = \left[ S^\dagger T_{13}^0 T_{12} \begin{pmatrix} E_1 & 0 & 0 \\ 0 & E_2 & 0 \\ 0 & 0 & E_3 \end{pmatrix} T_{12}^\dagger T_{13}^{0\dagger} S + \begin{pmatrix} V_c & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \right] \begin{pmatrix} \Psi_e \\ \tilde{\Psi}_\mu \\ \tilde{\Psi}_\tau \end{pmatrix}$$

vacuum term

matter term

# The Mikheev-Smirnov-Wolfenstein effect

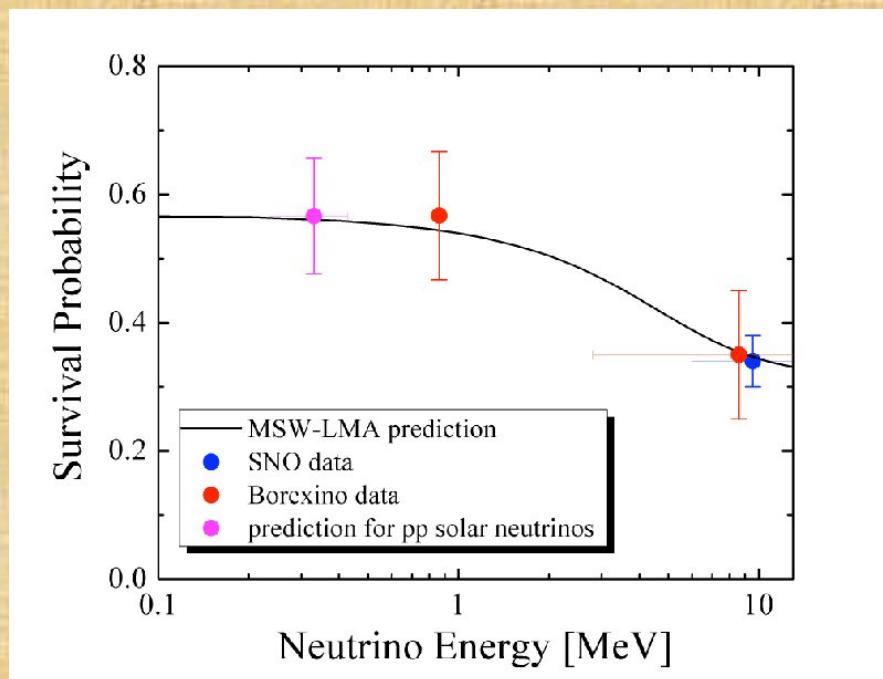


Flavour conversion is efficient if :

- the resonance condition is met ;
- the evolution at resonance is adiabatic.

The density profile, the neutrino energy and the mixing parameters say if the conversion is adiabatic/non-adiabatic.

## Experimentally observed !



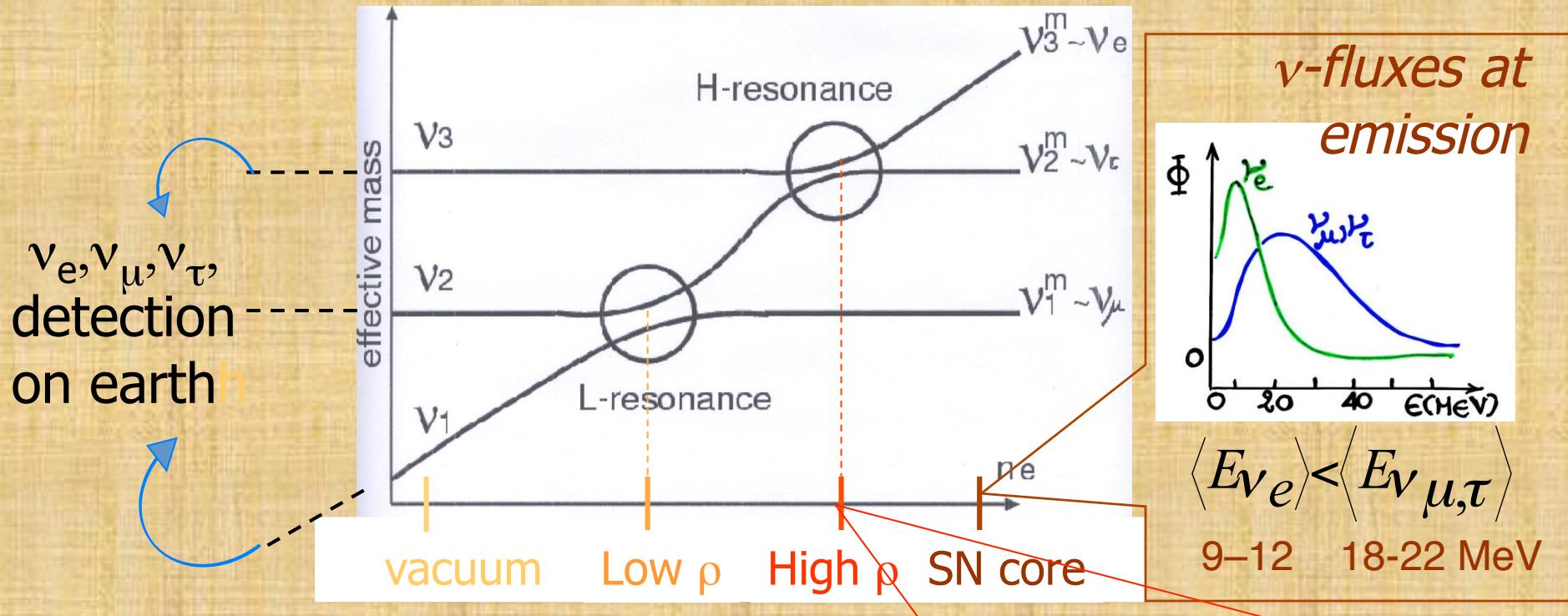
**the beautiful explanation of  
the « solar neutrino deficit »  
problem.**

Borexino Collaboration, J. Conf. Ser. 202, 012028 (2010)

# The MSW effect in supernovae

The MSW effect is encountered twice (three times) :

Dighe and Smirnov, PRD62(2000)033007



The hopping probability  $P_H$  :

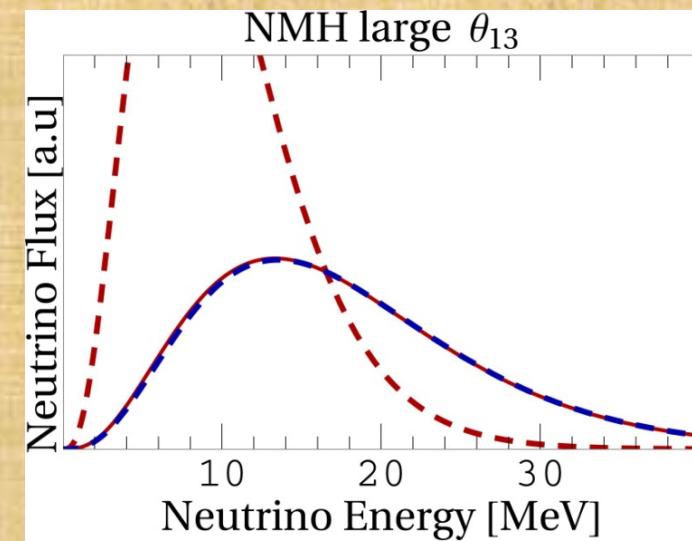
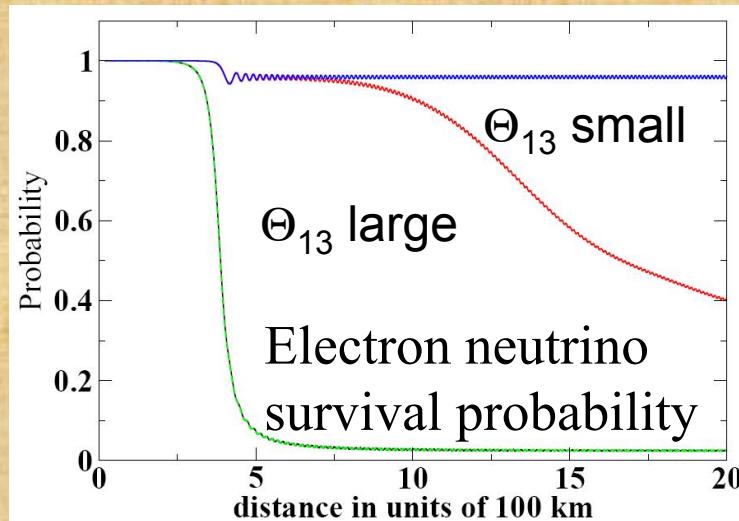
$$P_H = \exp \left[ -2\pi r_H \frac{\Delta m^2}{2E} \sin^2 \theta_{13} \right]$$

If  $\sin^2 2\theta_{13} \gg 10^{-3}$   $P_H = 0$   $\nu_e \rightarrow \nu_3$

If  $\sin^2 2\theta_{13} \ll 10^{-3}$   $P_H = 1$   $\nu_e \rightarrow \nu_2$

THE FLAVOUR CONVERSION AT THE HIGH RESONANCE DEPENDS  
ON THE NEUTRINO MASS HIERARCHY AND ON  $\theta_{13}$ .

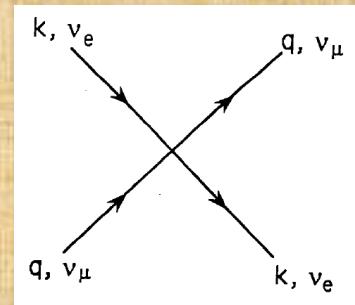
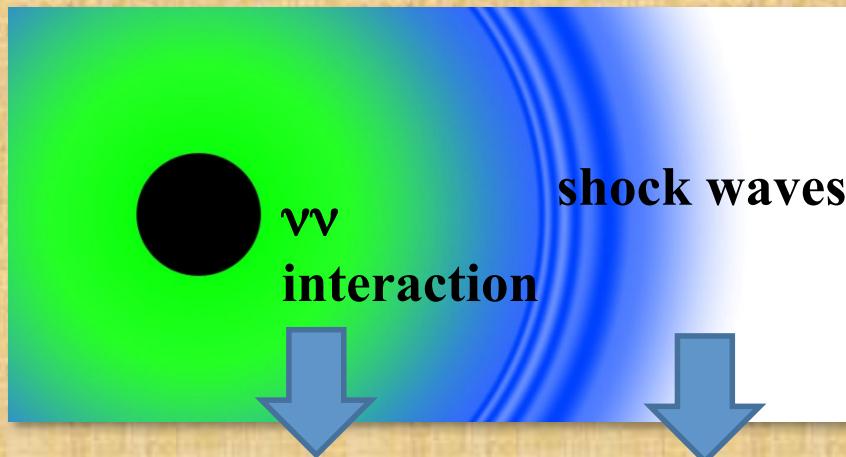
A numerical example :



Important impact on the fluxes.

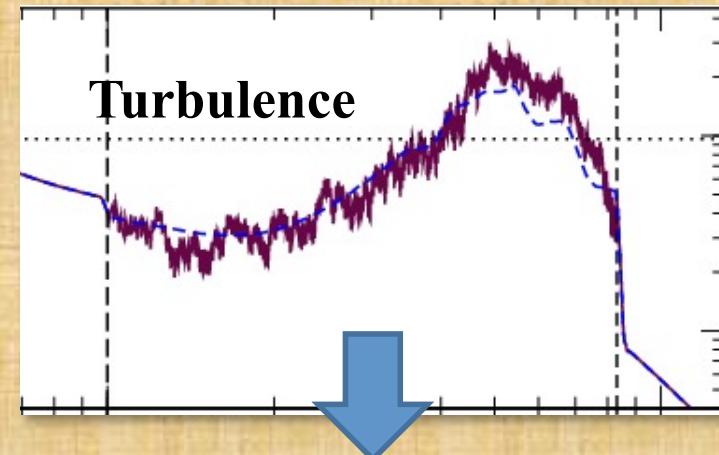
# Neutrino flavour conversion in SN

The case of core-collapse supernovae turns out to be much more complex : new flavour conversion phenomena emerge.



Collective flavour conversion effects

Multiple MSW resonances



New features arise

Understanding the different facets of flavour conversion in SN : the object of intense investigation.

## Turbulence

## shock waves

J. Pantaleone, PLB 287 (1992), Samuel, PRD 48 (1993), Sigl and Raffelt NPB 406 (1993), Pastor, Raffelt, Semikoz, PRD 65 (2002), Qian and Fuller, PRD 52 (1995) , Balantekin and Yuksel, New. J. Phys. 7 (2005), Duan, Fuller, Qian PRD74 (2006), PRL 97 (2006), PRD 75, 76 (2007), PRL 2008, PRD77 (2008), Fogli, Lisi, Mirizzi, Marrone, JCAP 2007, Raffelt and Smirnov, PRD 76 (2007), Estebal et al PRD 76 (2007), Gava and Volpe PRD(2008), Kneller, Gava, Volpe, McLaughlin (2009), Dasgupta, Dighe, Raffelt, Smirnov, PRL103(2009) , Dasgupta, Mirizzi, Tamborra, Tomas, PRD81 (2010), Fogli, Lisi, Marrone, Tamborra, JCAP0910(2009), ...

## $\nu\nu$ interaction

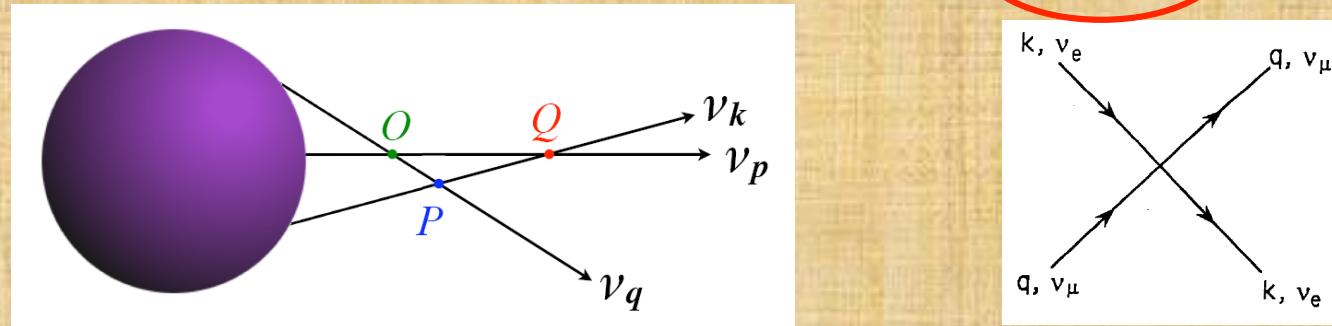
R. C. Schirato and G. M. Fuller (2002), arXiv : 0205390, C. Lunardini and A. Y. Smirnov, JCAP 0306, 009 (2003), 0302033, K. Takahashi, K. Sato, H. E. Dalhed, and J. R. Wilson, Astropart. Phys. 20, 189 (2003), 0212195, G. L. Fogli, E. Lisi, A. Mirizzi, and D. Montanino, Phys. Rev. 68, 033005 (2003), 0304056., R. Tomas, M. Kachelrieß, G. Raffelt, A. Dighe, H.-T. Janka, and L. Scheck, JCAP 0409, 015 (2004), 0407132., G. L. Fogli, E. Lisi, A. Mirizzi, and D. Montanino, JCAP 4, 2 (2005), 0412046., S. Choubey, N. P. Harries, and G. G. Ross, Phys. Rev. D74, 053010 (2006), 0605255., B. Dasgupta and A. Dighe, Phys. Rev. 75, 093002 (2007), 0510219., S. Choubey, N. P. Harries, and G. G. Ross, Phys. Rev. 76, 073013 (2007), 0703092., J. P. Kneller, G. C. McLaughlin, and J. Brockman, Phys. Rev. 77, 045023 (2008), 0705.3835., J. P. Kneller and G. C. McLaughlin, Phys. Rev. 73, 056003 (2006), 0509356., S. Galais, J. Kneller, C. Volpe and J. Gava, PRD(2010), ...  
Loreti et al, PRD 52 (1995); Balantekin et al, PRD 54 (2006), Friedland and Gruzinov, hep/0607244, Fogli et al JCAP 0606 (2006);. Kneller ,arXiv: 1004.1288, J. P. Kneller and C. Volpe, PRD (2010), arXiv: 1006.0913, ...

# The $\nu$ - $\nu$ interaction

J. Pantaleone, PLB 287 (1992), Samuel, PRD 48 (1993), Sigl and Raffelt, NPB 406 (1993),

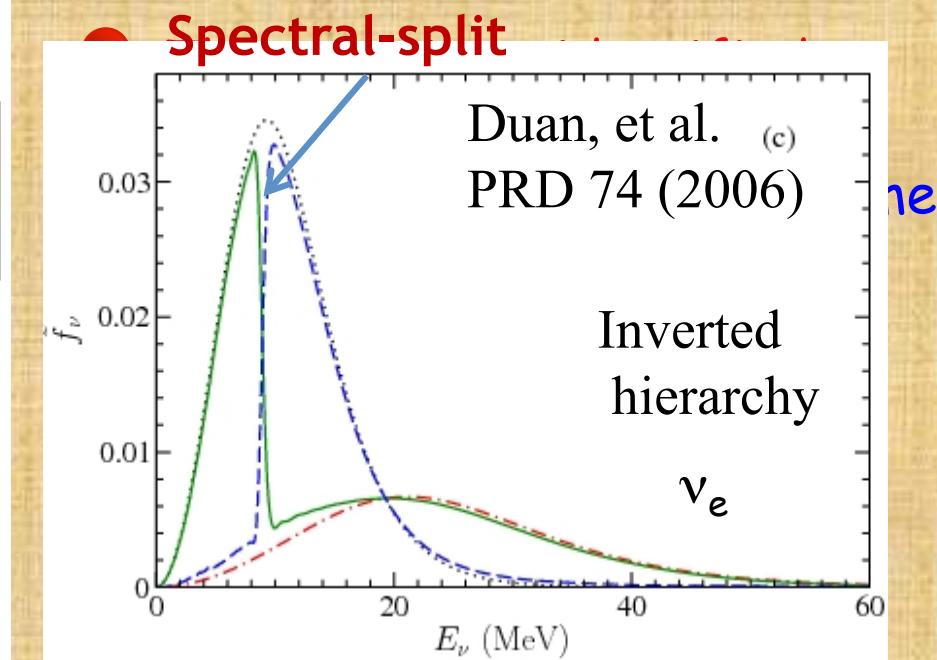
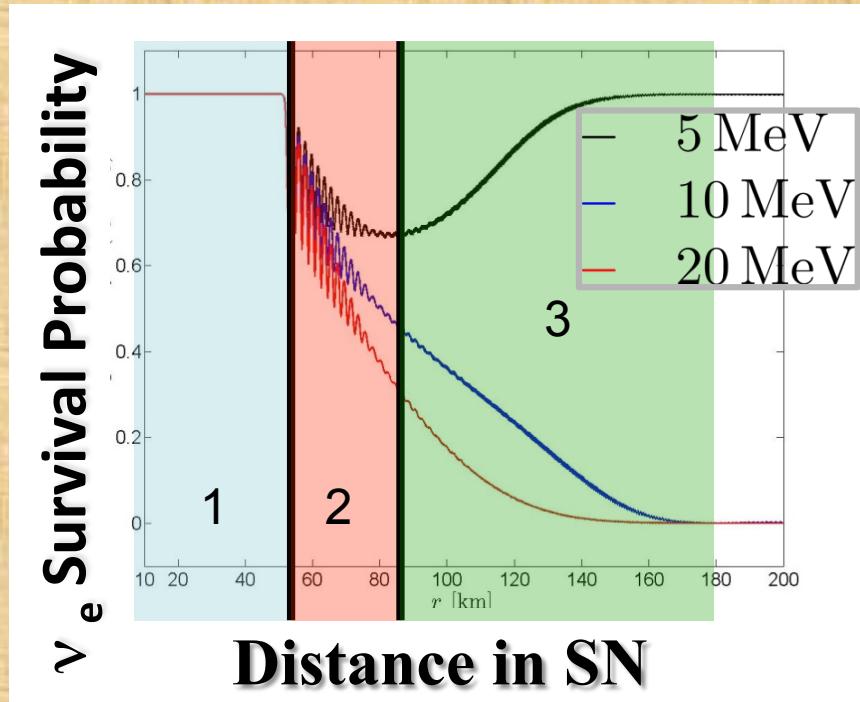
- Important progress since 2006 : Duan, Fuller, Qian PRD74 (2006)  
the inclusion of the neutrino-neutrino interaction modifies significantly the neutrino propagation in matter.

$$H = H_{\text{vacuum}} + H_{\text{matter}} + H_{\nu\nu}(\rho_\nu)$$



- Involved numerically : large number of coupled stiff non-linear equations.

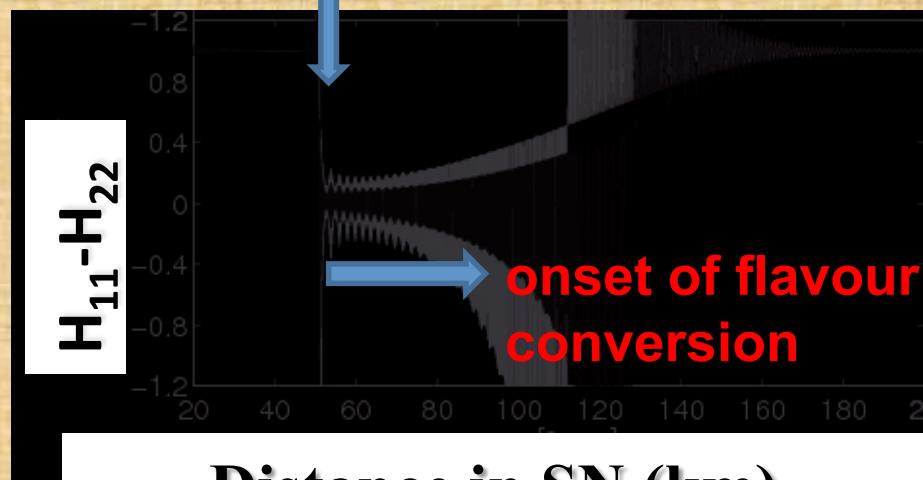
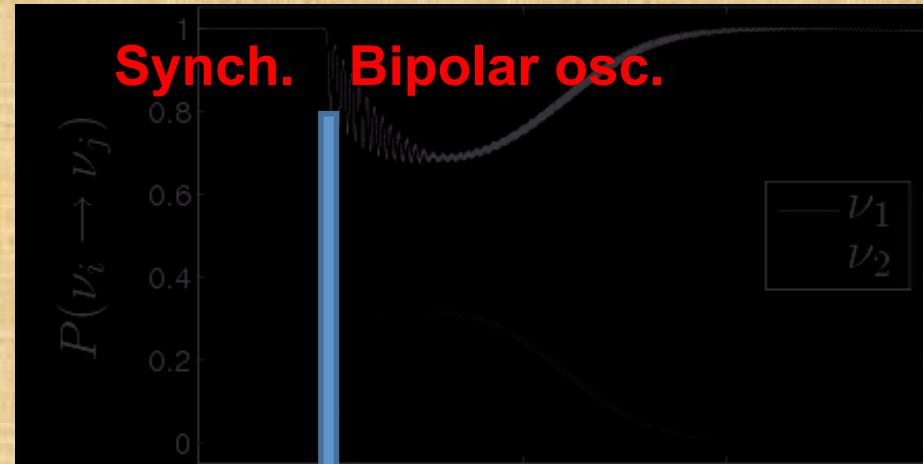
# Neutrino flavour conversion triggered by the $\nu\nu$ -interaction



Important modifications of  $\nu$ -fluxes,  
near the neutrinosphere

# The role of the matter phase

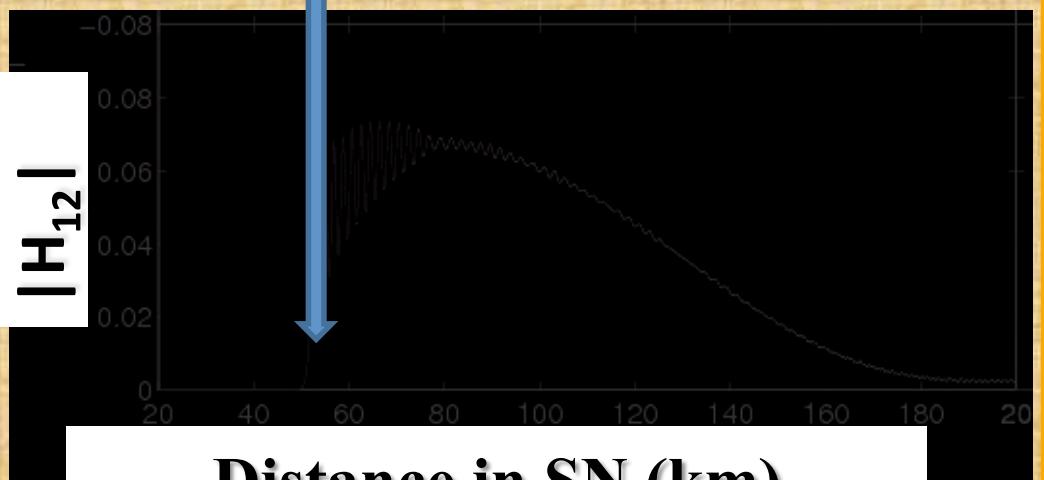
S. Galais, J. P. Kneller , C. Volpe, arXiv: 1102.1471



In 2ν flavors the matter Hamiltonian :

$$\tilde{\mathbf{H}} = \begin{pmatrix} \mathbf{H}_{11} & \mathbf{H}_{12} \\ \mathbf{H}_{12}^* & \mathbf{H}_{22} \end{pmatrix}$$

The phase derivative contributes to diagonal & off-diagonal terms.



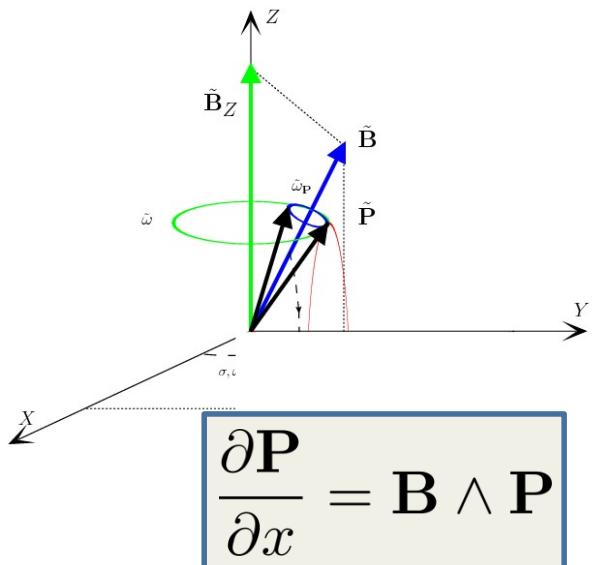
Distance in SN (km)

Distance in SN (km)

The onset of bipolar oscillations due to a rapid growth of the phase derivative.

# Understanding the dynamics using the polarization vector formalism

## Polarization vector formalism

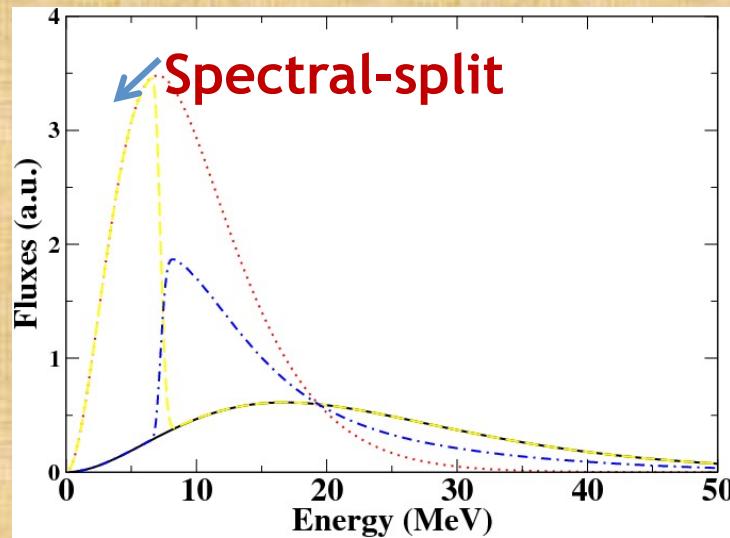


$$\mathbf{B} = \begin{pmatrix} 2\mathcal{R}(H_{e\mu}) \\ -2\mathcal{I}(H_{e\mu}) \\ H_{ee} - H_{\mu\mu} \end{pmatrix} \quad \mathbf{P} = \begin{pmatrix} 2\mathcal{R}(\psi_e \psi_\mu^*) \\ -2\mathcal{I}(\psi_e \psi_\mu^*) \\ |\psi_e|^2 - |\psi_\mu|^2 \end{pmatrix}$$

## Example : Flavor basis

The neutrino evolution with the neutrino polarization vectors : the precession of an effective spin around an effective magnetic field.

## Many aspects unravelled



**Open questions remain,  
e.g. for the spectral  
split phenomenon a  
comprehensive understanding  
is still missing...**

- **A flavour pendulum (nutation):**

Duan, Fuller, Qian, PRD 74(2006)

- **A gyroscopic flavour pendulum (precession and nutation):**

Hannestad, Raffelt, Sigl, and Wong,  
Phys. Rev. D74, 105010 (2006), 0608695.

- **The spectral split as a precession solution :**

Duan, Fuller, Qian, PRD76(2007)  
Meng and Qian, PRD (2011)

- **An adiabatic MSW like evolution in  
the comoving frame :**

Raffelt and Smirnov PRD 76 (2007), PRL 2007

- **The extention to three flavours (SU(3)) :**

Dasgupta and Dighe PRD (2007)

- **There can be single and multiple splits depending  
on the neutrino flux ratios at the neutrinosphere:**

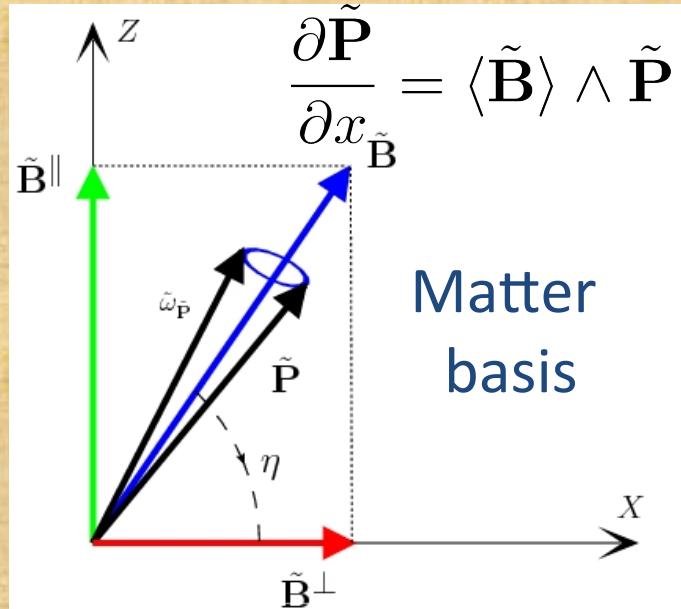
Dasgupta, Dighe, Raffelt, Smirnov, PRL103(2009)

Dasgupta, Mirizzi, Tamborra, Tomas, PRD81 (2010),  
Fogli, Lisi, Marrone, Tamborra, JCAP0910(2009)

- **It can be described as a system of quasi-particles :**

Pehlivan, Balantekin, Kajno, Toshida, arXiv:1105.1182

# The spectral split: a magnetic resonance phenomenon

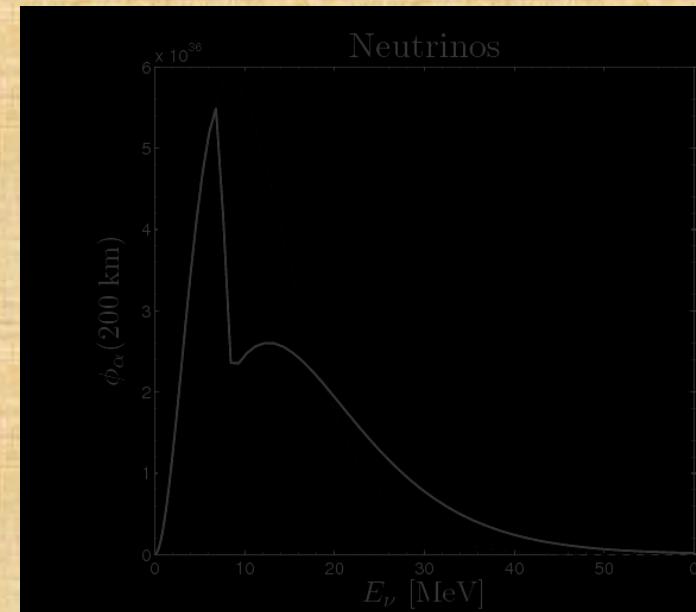
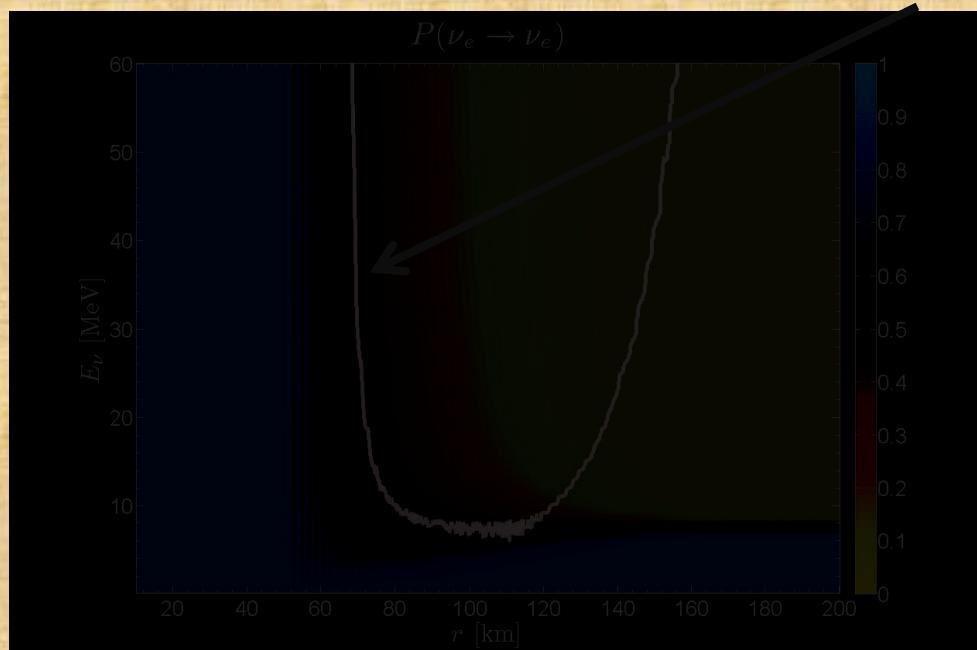


Galais and Volpe, to appear in PRD, arXiv:1103.5302 .

The magnetic resonance phenomenon is the spin inversion occurring when the frequency of the magnetic field in the plane is close to the spin precession frequency around  $B_z$ .

The magnetic resonance condition :

$$\omega - \omega_0 = 0 \quad (\omega - \omega_0)/\omega_1 \ll 1$$

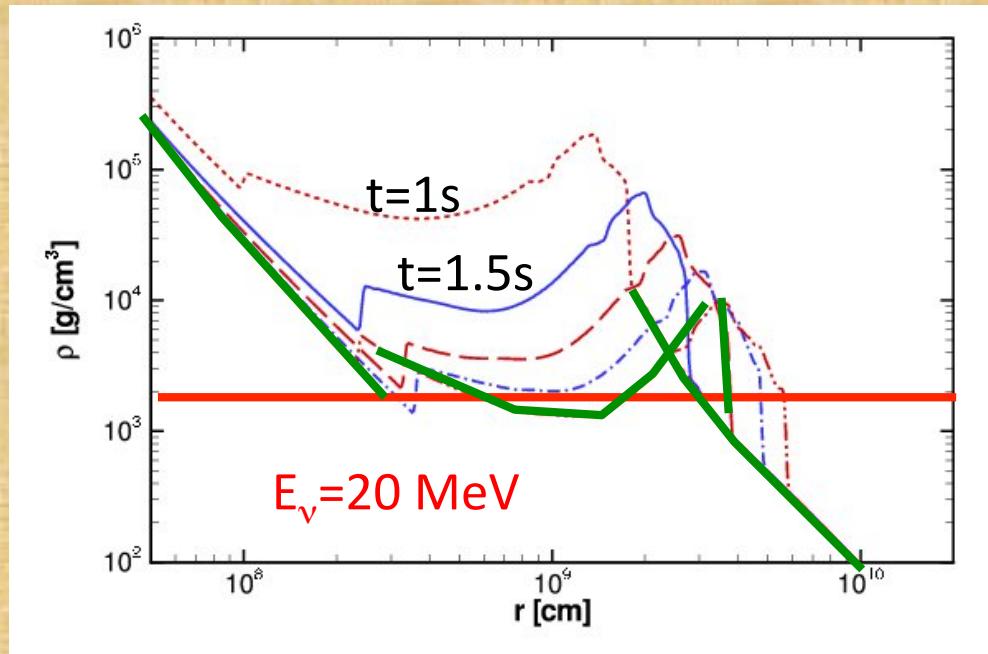


THE MAGNETIC RESONANCE CONDITION IS FULFILLED.

# The shock wave effects

Neutrino evolution for a density profile including shock waves

1. Before the shock (adiabatic  $\nu$  propagation).
2. The shock arrives (non-adiabatic prop.).
3. Phase effects appear.
4. Post-shock propagation.

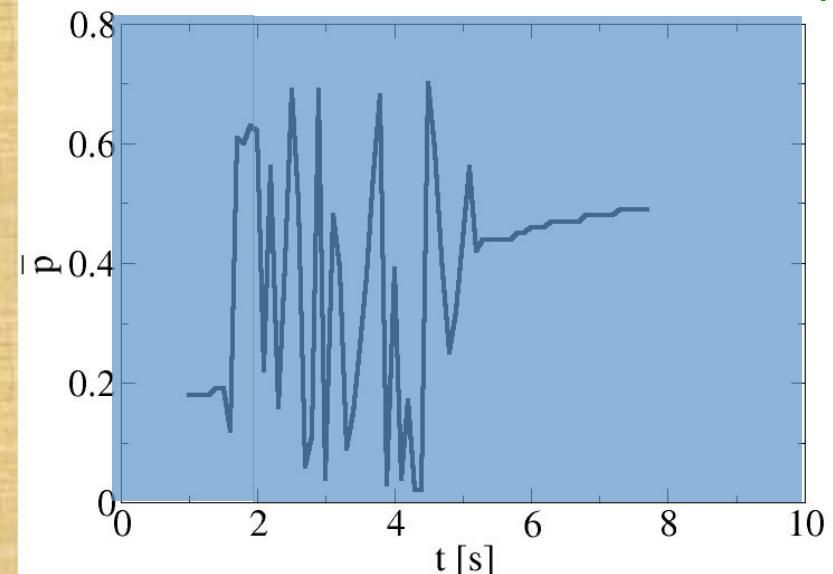


J. P. Kneller, G. C. McLaughlin, J. Brockman,  
PRD 77, 045023 (2008).

B. Dasgupta and A. Dighe, Phys. Rev. 75,  
093002 (2007), 0510219.

Schirato and Fuller (2002), arXiv : 0205390.

inverted hierarchy, large  $\theta_{13}$



S. Galais et al., PRD 81 (2010) 053002,  
arXiv :0906.5294.

MULTIPLE RESONANCES AND  
PHASE EFFECTS APPEAR.

# CP violation effects in astrophysics and cosmology (BBN epoch)



## Solar neutrinos

H.Minakata and S. Watanabe, Phys. Lett. B 468, 256 (1999).



## Core-collapse supernova neutrinos

E. Akhmedov, C.Lunardini & A.Smirnov, Nucl.Phys.B643 (2002) 339.

A. B. Balantekin, J. Gava, C. Volpe, PLB662, 396 (2008), arXiv:0710.3112.

J. Gava, C. Volpe, Phys. Rev. D78, 083007(2008), arXiv:0807.3418.

J Kneller and G.C. McLaughlin, PRD 80,053002 (2009) arXiv:0904.3823.



## Cosmological neutrinos

J. Gava, C. Volpe, Nucl. Phys. B (2010), arXiv:1002.0981 .

# CP violation and core-collapse SN

A. B. Balantekin, J. Gava, C. Volpe, PLB662, 396 (2008), arXiv:0710.3112  
 J. Gava, C. Volpe, Phys. Rev. D78, 083007(2008), arXiv:0807.3418.

- We have demonstrated under which conditions there can be CP violating effects in supernovae. Here the main steps :

$$U = T_{23} S^\dagger T_{13}^0 S T_{12} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & e^{i\delta} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13} \\ 0 & 1 & 0 \\ -s_{13} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & e^{-i\delta} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

The neutrino evolution equations in matter are

$$i \frac{\partial}{\partial t} \begin{pmatrix} \Psi_e \\ \tilde{\Psi}_\mu \\ \tilde{\Psi}_\tau \end{pmatrix} = \left[ S^\dagger T_{13}^0 T_{12} \begin{pmatrix} E_1 & 0 & 0 \\ 0 & E_2 & 0 \\ 0 & 0 & E_3 \end{pmatrix} T_{12}^\dagger T_{13}^{0\dagger} S + \begin{pmatrix} V_c & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \right] \begin{pmatrix} \Psi_e \\ \tilde{\Psi}_\mu \\ \tilde{\Psi}_\tau \end{pmatrix}$$

vacuum term

matterterm

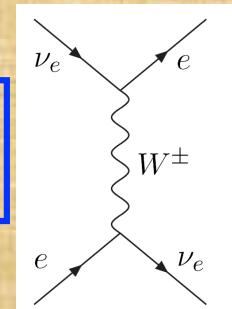
with

$$\tilde{\Psi}_\mu = \cos \theta_{23} \Psi_\mu - \sin \theta_{23} \Psi_\tau \text{ and } \tilde{\Psi}_\tau = \sin \theta_{23} \Psi_\mu + \cos \theta_{23} \Psi_\tau$$

$$S^\dagger = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & e^{i\delta} \end{pmatrix}$$

the T23 basis

factorizes out easily and gives:



# CP violation effect in SN

$$\tilde{H}(\delta) = S^\dagger \tilde{H}(\delta = 0) S$$

$$\tilde{U}(\delta) = S^\dagger \tilde{U}(\delta = 0) S$$

Evolution operator  
in the  $T_{23}$  basis

This leads to the two following relations:

$$P(\nu_e \rightarrow \nu_e, \delta \neq 0) = P(\nu_e \rightarrow \nu_e, \delta = 0)$$

$$P(\nu_\mu \rightarrow \nu_e, \delta \neq 0) + P(\nu_\tau \rightarrow \nu_e, \delta \neq 0) = P(\nu_\mu \rightarrow \nu_e, \delta = 0) + P(\nu_\tau \rightarrow \nu_e, \delta = 0)$$

The electron neutrino flux in the SN:

$$\phi_{\nu_e}(\delta) = L_{\nu_e} P(\nu_e \rightarrow \nu_e) + L_{\nu_\mu} P(\nu_\mu \rightarrow \nu_e) + L_{\nu_\tau} P(\nu_\tau \rightarrow \nu_e)$$

$$\phi_{\nu_e}(\delta) = L_{\nu_e} P(\nu_e \rightarrow \nu_e) + L_{\nu_\mu} (P(\nu_\mu \rightarrow \nu_e) + P(\nu_\tau \rightarrow \nu_e))$$
$$\neq f(\delta)$$
$$\neq f(\delta)$$

At tree level no CP effects, however ...

# Effects from the Dirac phase in SN

$$\tilde{H}(\delta) \neq S^\dagger \tilde{H}(\delta = 0)S$$

The  $\nu$  propagation Hamiltonian does not factorize any more !

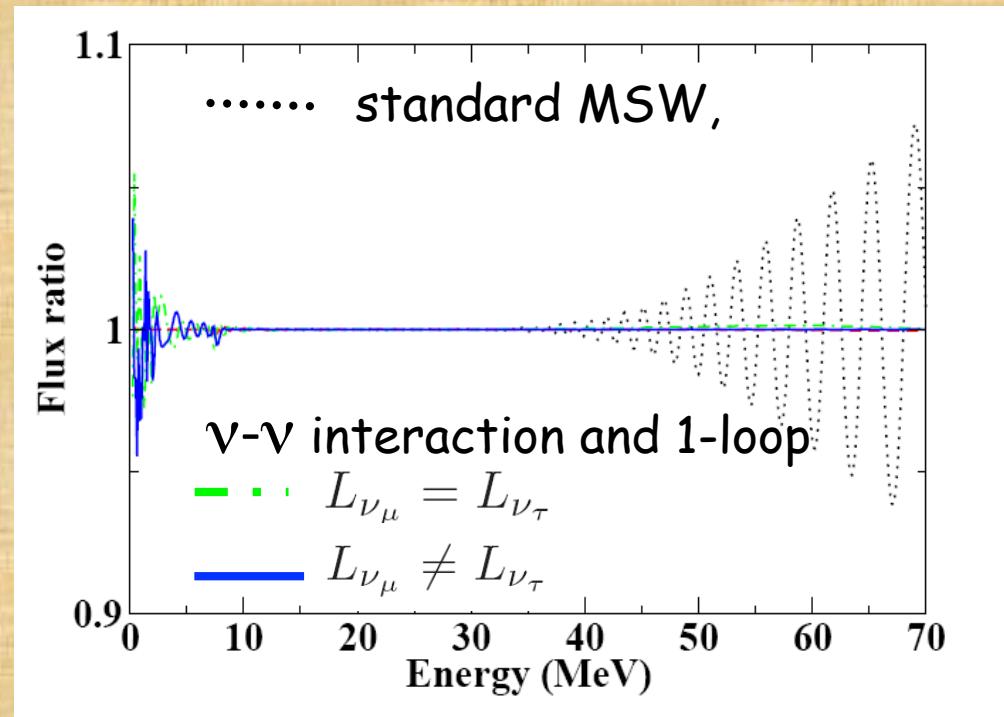
$$L_{\nu_\mu} \neq L_{\nu_\tau} \text{ at the neutrinosphere}$$

In the Standard Model loop corrections for the  $\nu$  interaction with matter should be included.

Beyond the Standard Model might introduce differences in the  $\nu_\mu$  and  $\nu_\tau$  interaction with matter (Flavor Changing Neutral Currents, ...).

**THERE CAN BE CP-VIOLATION EFFECTS IN SUPERNOVAE.**

# Numerical results



Gava, Volpe, Phys. Rev. D78 (2008),  
arXiv:0807.3418

EFFECTS OF 5% ON THE ELECTRON NEUTRINO FLUXES.

*Further investigations are needed  
to assess the impact on observations,  
likely to be small...*

# OUTLINE

☀️ Observations : learning  
about supernova dynamics  
and neutrino properties

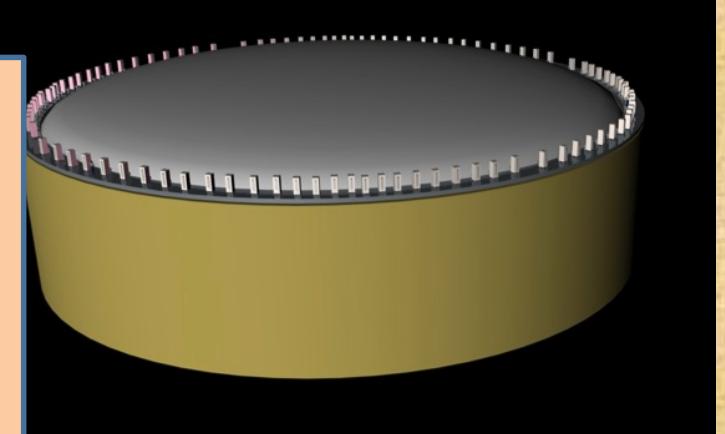
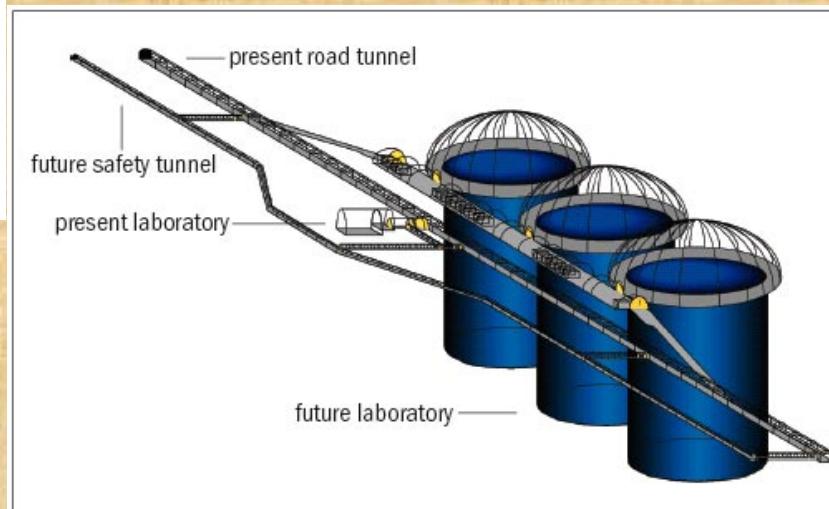
# Observations

A SN neutrino signal



## THE DSNB

We want to observe  
the diffuse  
supernova neutrino  
background  
- Gd-doping and  
Megaton detectors .



## Nucleosynthesis

Neutrinos play a key  
role in various  
nucleosynthesis  
processes, in  
particular the  
r-process or the  
neutrino process.

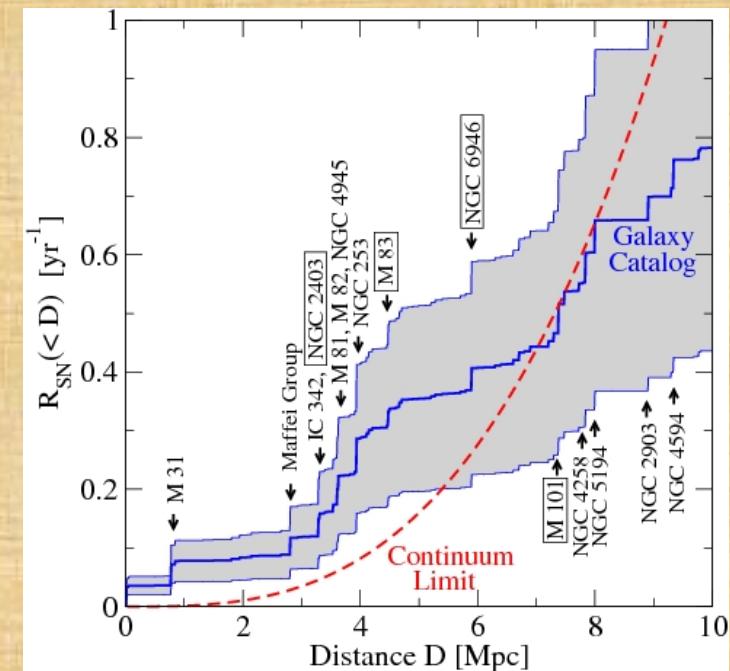
*Different observations complementary.*

# Future SN observations

Several detectors are running (ex. Borexino, Kamland, Super-K,...). Large-size detectors are under study : LAGUNA DS, FP7, 2008-2010 and LAGUNA LBNO, 2011-2013).

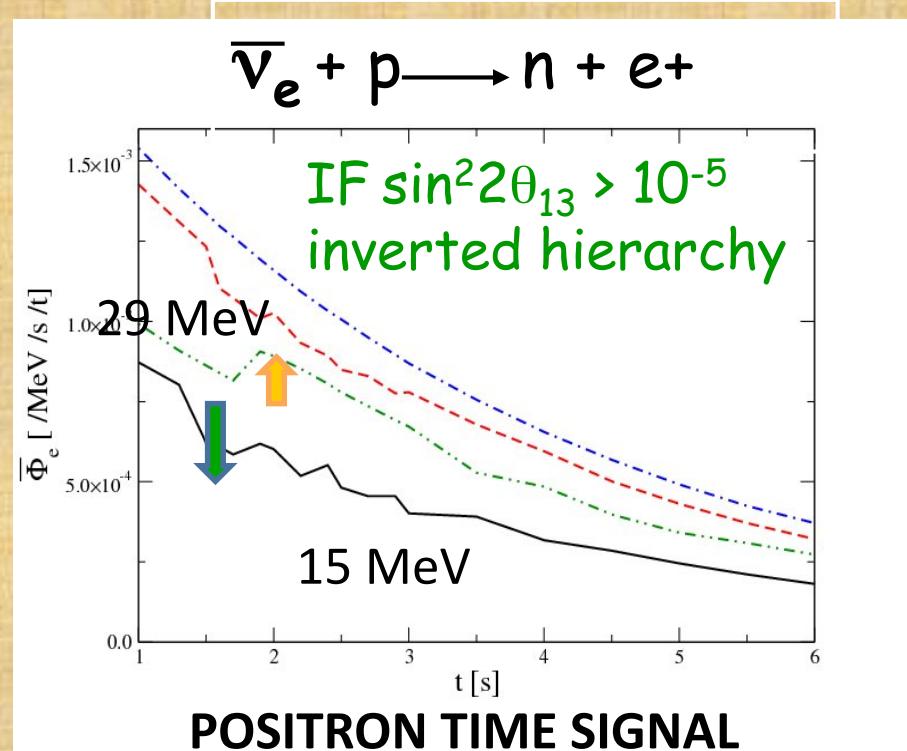
I. To measure the neutrino luminosity curve from a future (extra)galactic explosion (ex.  $10^5$  events in MEMPHYS).

II. To measure the diffuse supernova neutrino background (sensitive to the star formation rate as well).

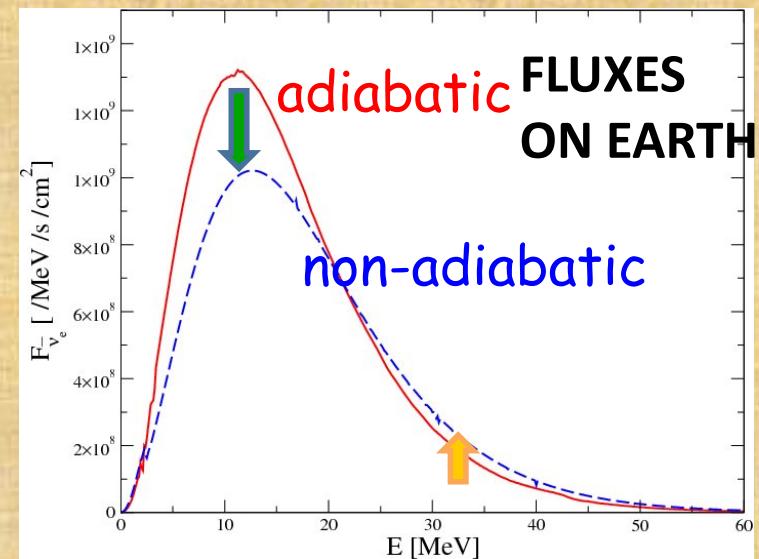


Ando,Beacom,Yuksel PRL95 (2005)

# An imprint of the shock on the time signal, depending on $\nu$ -properties



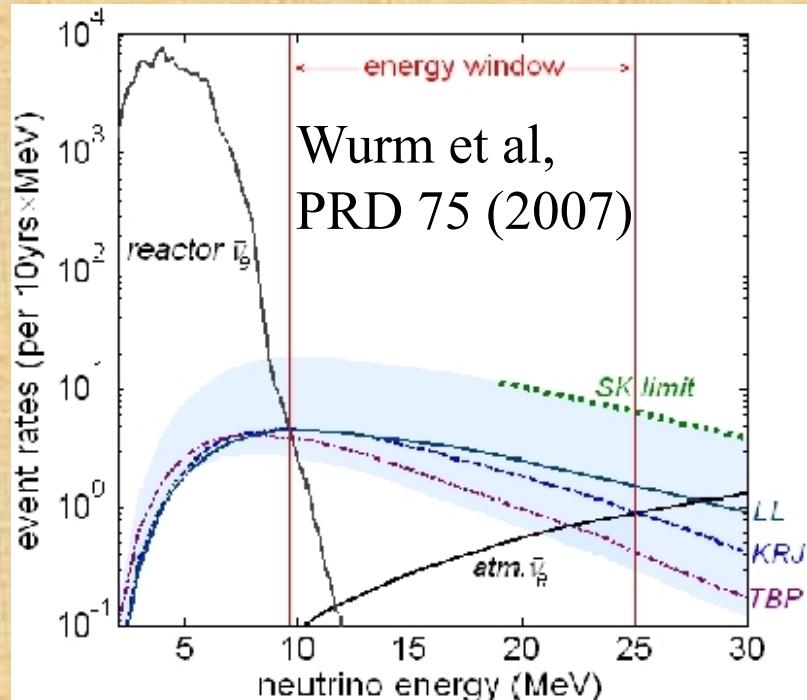
First calculation including  
the  $\nu$ - $\nu$  interaction and  
shock wave effects.



Gava, Kneller, Volpe, McLaughlin,  
PRL 103 (2009), arXiv:0902.0317

The bump (dip) can be seen at 3.5 (1) sigma in  
Super-Kamiokande if a supernova at 10 kpc explodes..

# DSNB event rates in $\nu$ -observatories



after 10 years

There is an energy window free from backgrounds, where neutrinos from past supernovae can be discovered either with advanced technologies or with large size observatories.

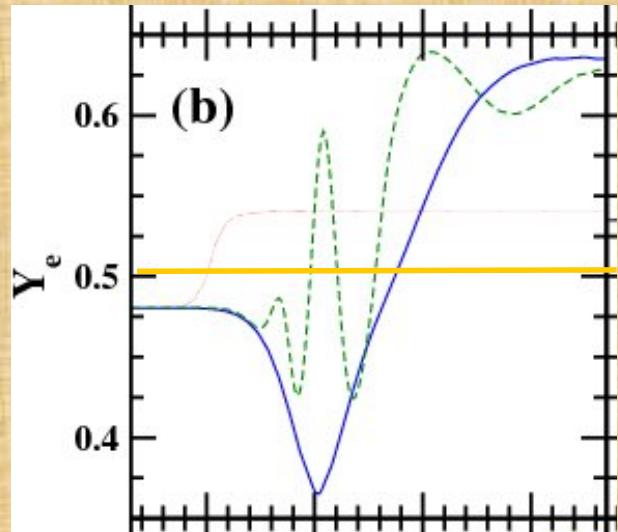
Argon detectors (100 kton).

Normal Hierarchy			
$N_{\text{events}}$	Detection window	L	S
$\nu_e$	17.5-41.5 MeV	<b>66</b>	<b>58</b>
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S. Galais, J. Kneller, C. Volpe, J. Gava, PRD 81(2010) 053002, arXiv :0906.5294.

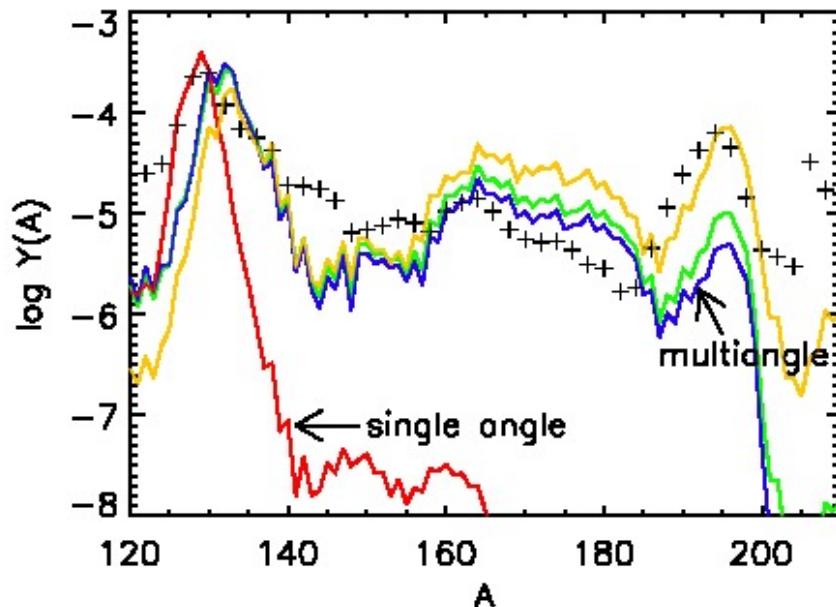
# Impact on nucleosynthesis of the $\nu\nu$ int.

Effect on the neutron/proton ratio



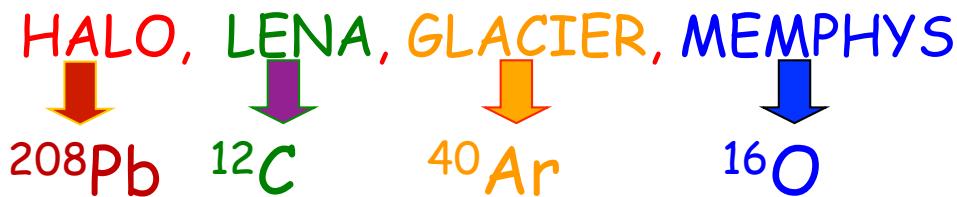
Yuksel and Balantekin,  
New J.Phys.7, 51(2005).

Chakraborty, Choubey,  
Goswami, Kar, JCAP 1006,  
007 (2010), arXiv:0911.1218.



Duan, Friedland, McLaughlin, Surman  
JPG 38,035201 (2010)

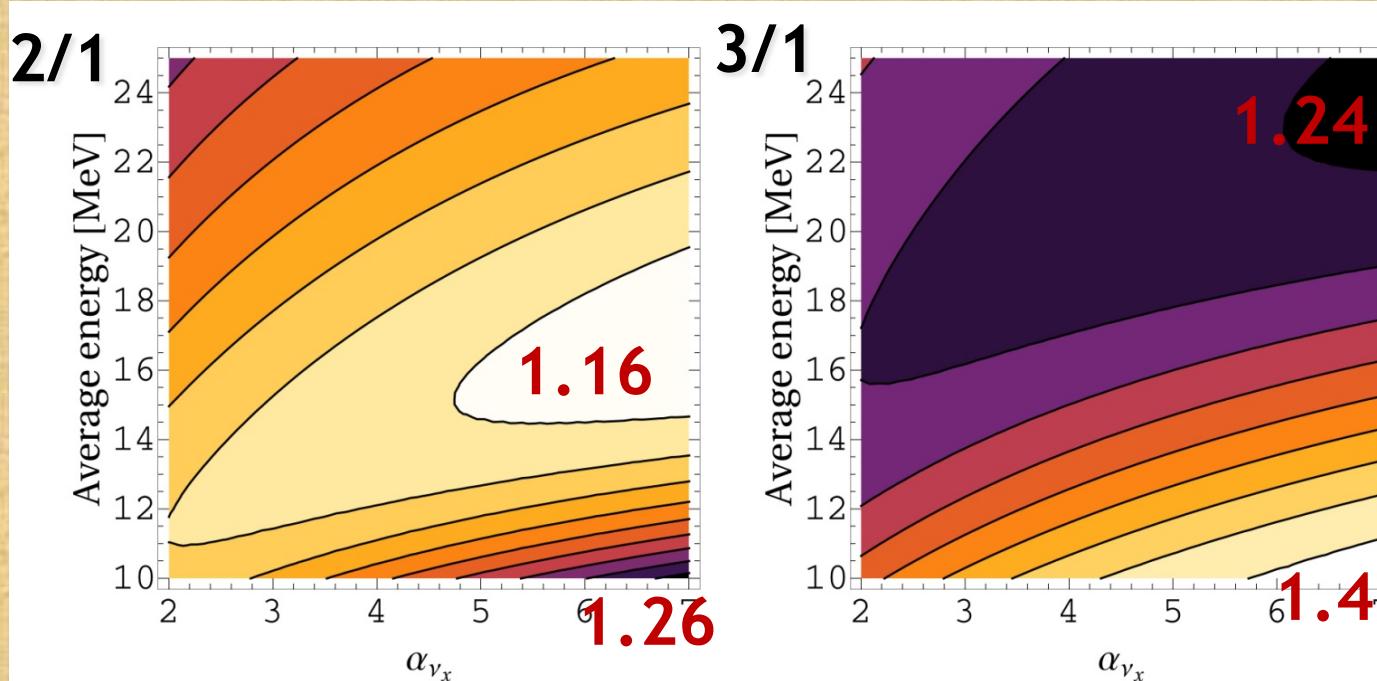
$\nu_e$  detection :  $\nu$ -nucleus cross sections necessary  
to determine the supernovae observatories's responses



# Low energy neutrino-nucleus cross section uncertainties

AN EXAMPLE

Ratio of flux-averaged cross sections



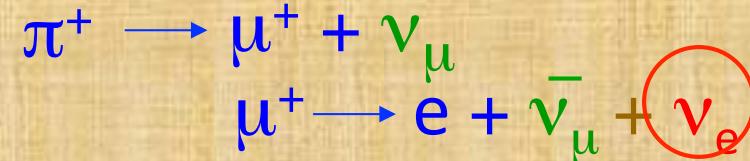
Neutrino-lead calculations used  
for the comparison:

- 1- J.Engel, et al. PRD 67, 013005 (2003) RPA
- 2- E. Kolbe *et al.*, PRC 63, 025802 (2001) CRPA
- 3- N. Paar (priv. communication) relativistic RPA

Neutrino-nucleus cross section measurements welcome...  
*also useful for double-beta decay (ga, forbidden,...)*

# POSSIBLE FUTURE INTENSE $\nu$ SOURCES

at SPALLATION SOURCES

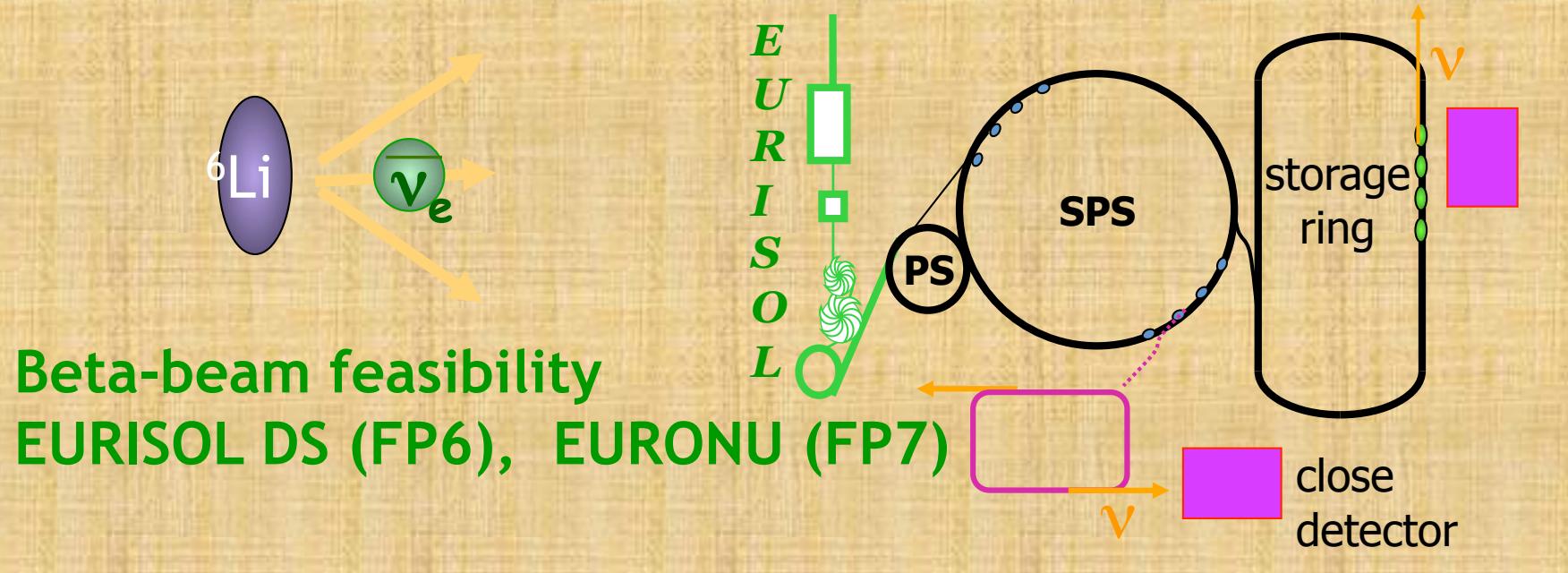


Future facilities : SNS, ESS, JSNS, SPL

Low energy BETA-BEAMS

C.Volpe, J Phys G 30 (2004) L1.

A proposal to establish a facility for the production of intense and pure low energy neutrino beams in the 100 MeV energy range.



## For the next (extra)galactic supernova explosion and the DSNB discovery

It is very important to have a network of detectors....

- sensitive to both electron anti-neutrinos and electron neutrinos, besides to neutral current.
- with very different energy thresholds, in particular for the  $\nu_e$  : argon-based (5 MeV), lead-based (10, 20 MeV), scintillators and Cherenkov (about 20 MeV).
- with good time resolution or time and energy resolution.
- at least one large size (megaton) detector.

# Conclusions and Perspectives

Supernova explosion on the way...

Neutrino flavour conversion processes  
in such explosive media has really  
increased in complexity.



The SN neutrino fluxes encode  
information on  $\nu$ -properties  
and supernova dynamics :

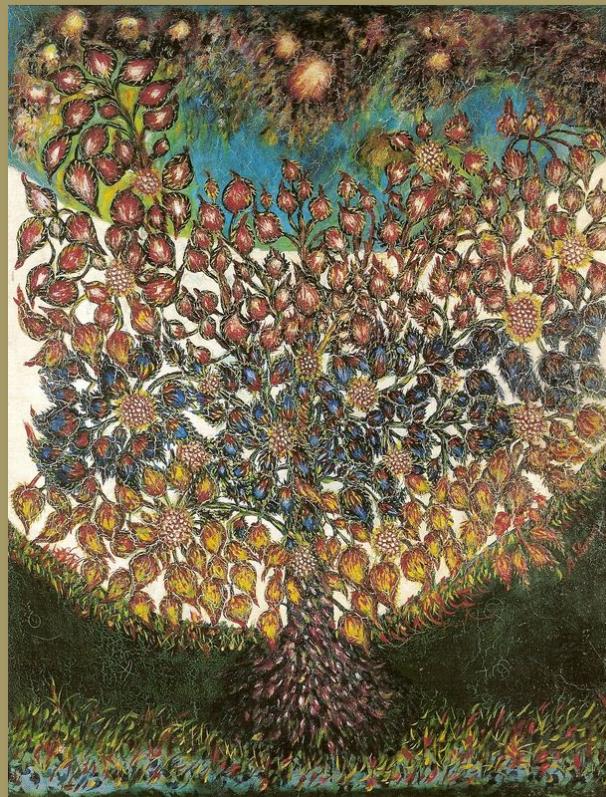


A lot to learn from future observations !

**Danke.**

**Thank you**

**Grazie**



**Life tree**

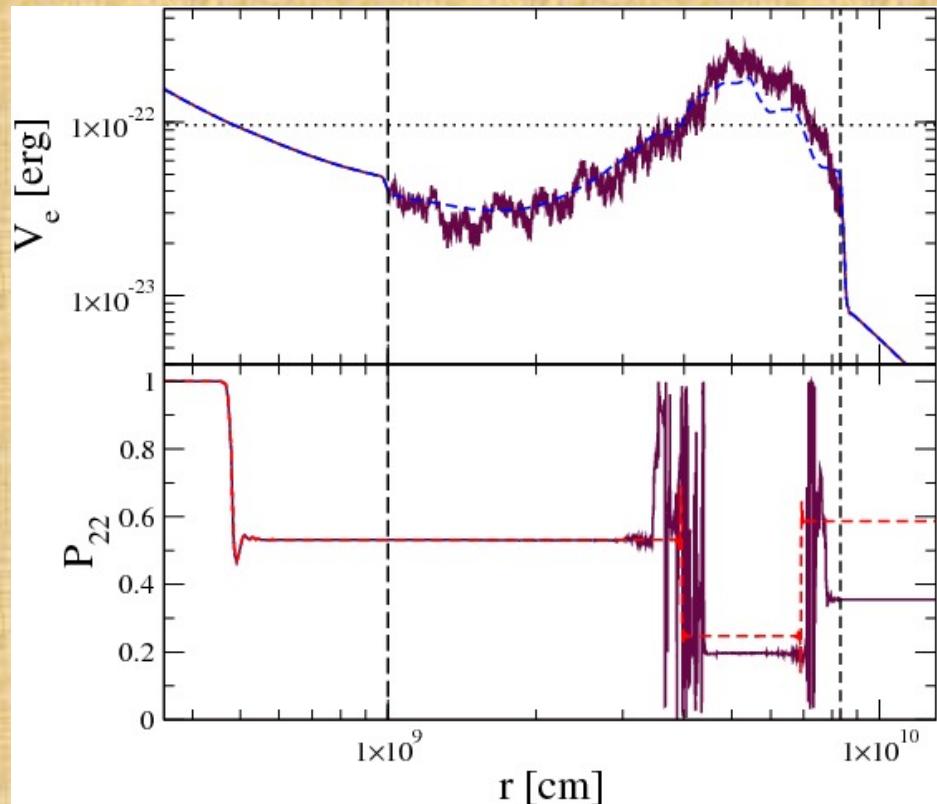
**Merci**

**Gracias**

# Turbulence effects

Loreti et al, PRD 52 (1995); Balantekin et al, PRD 54 (1006); Friedland and Gruzinov, hep/0607244, Fogli et al JCAP 0606 (2006); Kneller arXiv: 1004.1288.

Calculation of instantiations of the neutrino amplitudes- not of average probabilities - in presence of shock waves and turbulence.

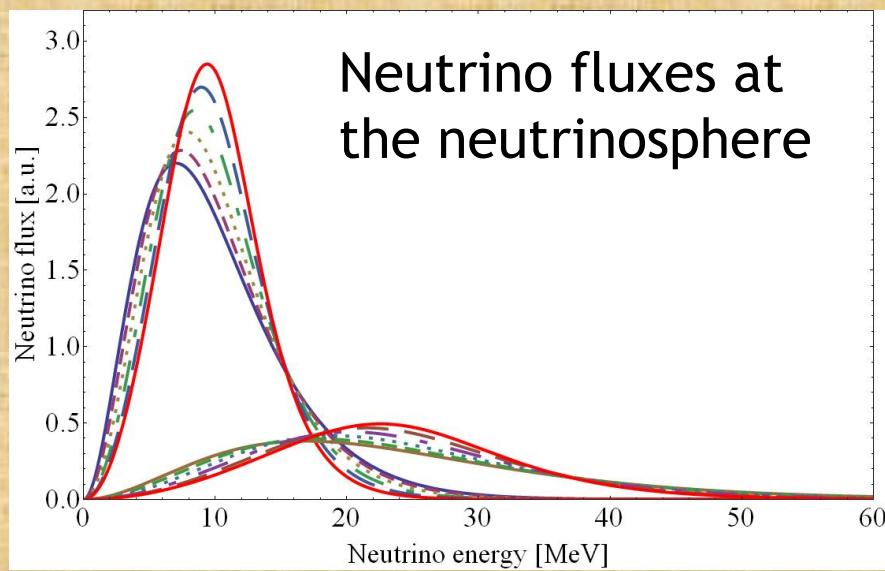


NEUTRINOS CAN COMPLETELY MIX («depolarize »).

TRANSITION FROM shock-wave to turbulence dominated regime, as the fluctuation amplitude increases.

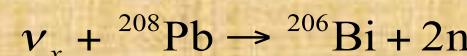
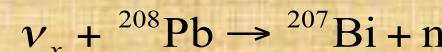
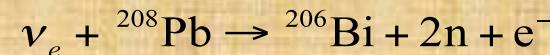
Kneller and Volpe, PRD (2010) , arXiv: 1006.0913 .

# The HALO project

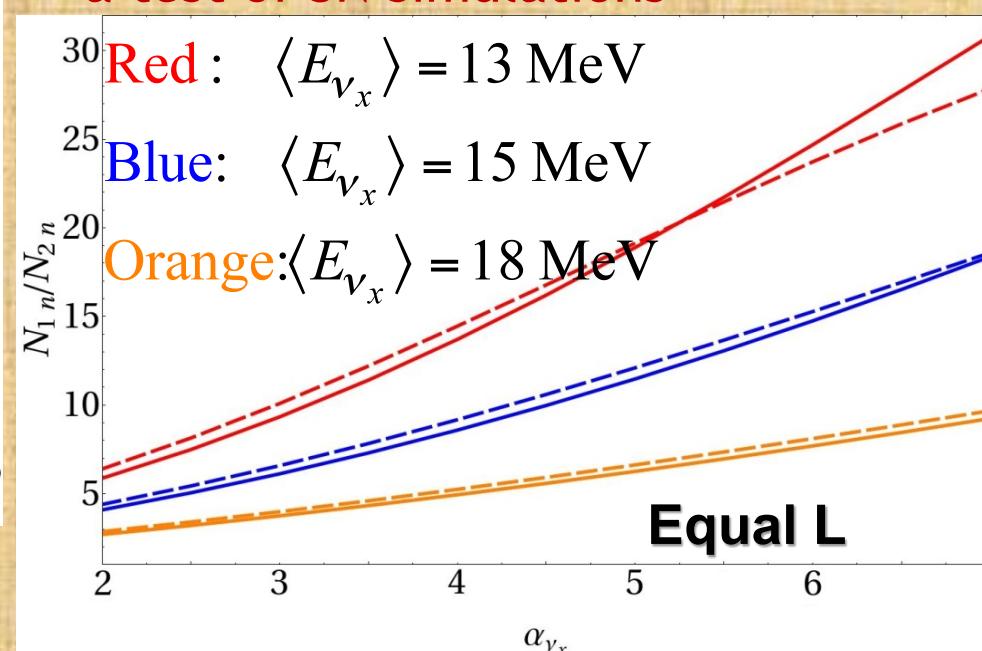


C. Volpe et, D. Vaananen to appear.

80 tonnes of Pb, HALO-2: 1kt



Information on the fluxes at the neutrinosphere can be extracted :  
a test of SN simulations



Important to have different energy thresholds.

# The role of the matter phase (derivative)

S. Galais, J. P. Kneller , C. Volpe, a

In 2v flavors the U matrix in matter :

$$\tilde{U} = \begin{pmatrix} 1 & 0 \\ 0 & e^{i\tilde{\beta}} \end{pmatrix} \begin{pmatrix} \cos \tilde{\theta} & \sin \tilde{\theta} \\ -\sin \tilde{\theta} & \cos \tilde{\theta} \end{pmatrix}$$

matter phase  $\longleftrightarrow$  matter angle

The matter phase since the hamiltonian off-diagonal terms

The v evolution equation

$$i \frac{\partial \tilde{\psi}}{\partial x} = \tilde{H} \tilde{\psi} = \left( \tilde{K} - i \tilde{U}^\dagger \frac{\partial \tilde{U}}{\partial x} \right) \tilde{\psi}$$

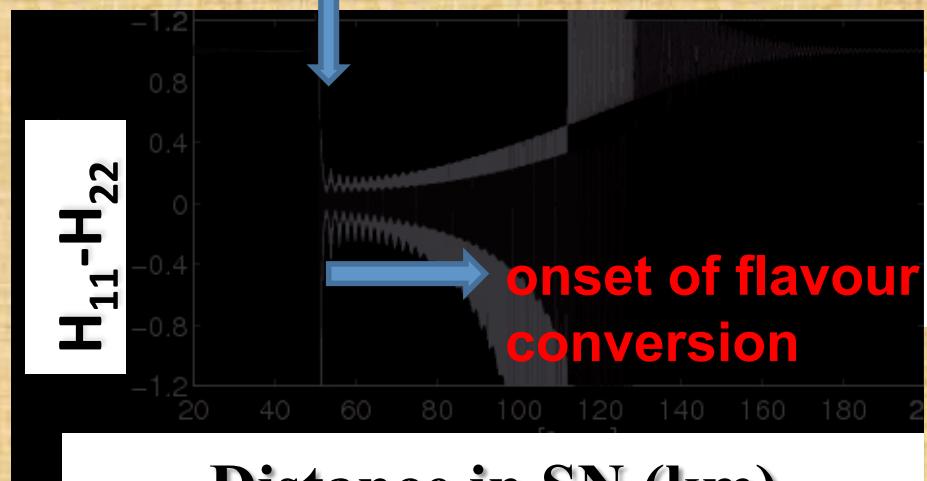
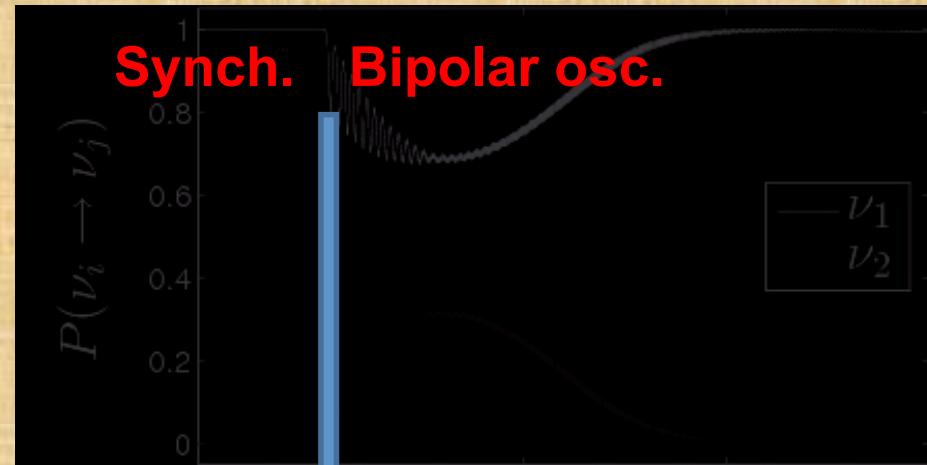
It involves the derivative of the matter phase.

$$\tilde{\mathbf{H}} = \begin{pmatrix} \mathbf{H}_{11} & \mathbf{H}_{12} \\ \mathbf{H}^*_{12} & \mathbf{H}_{22} \end{pmatrix}$$

The phase derivative contributes to diagonal & off-diagonal terms.

# The matter basis point of view : the phase derivative role

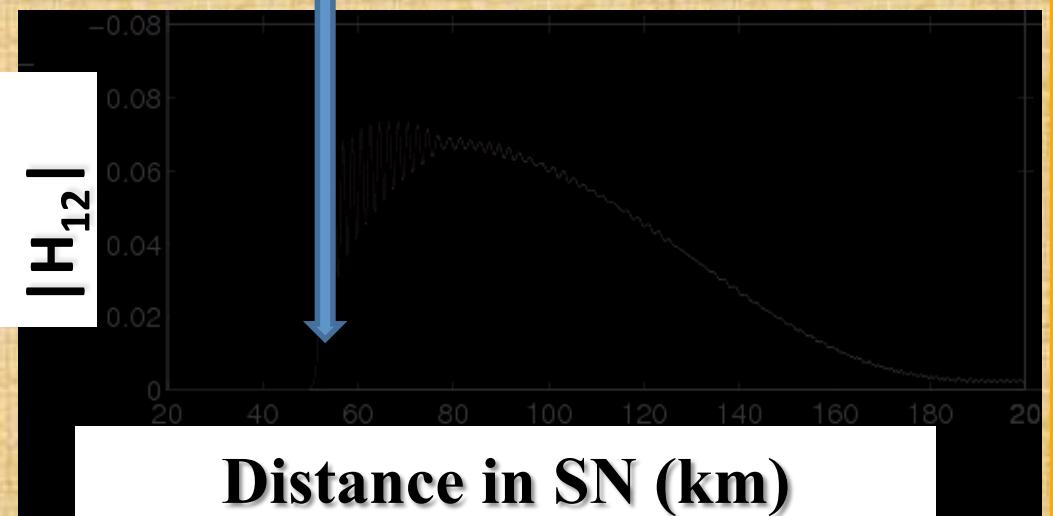
S. Galais, J. P. Kneller , C. Volpe, arXiv: 1102.1471



In 2ν flavors the matter Hamiltonian :

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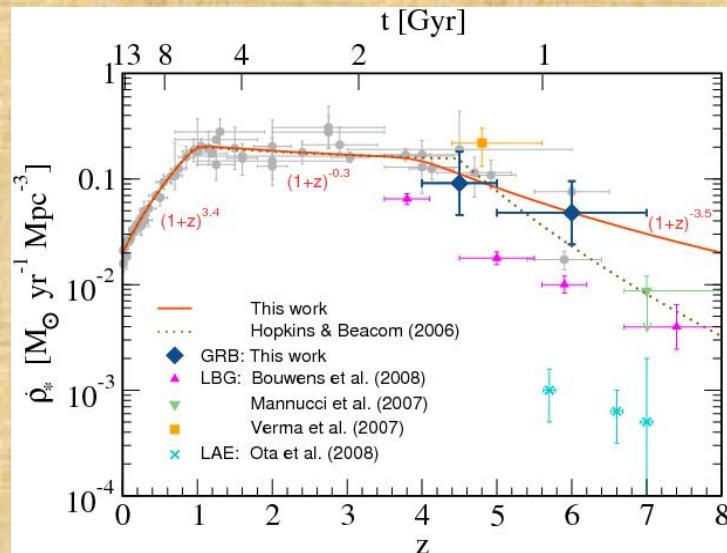


The onset of bipolar oscillations due to a rapid growth of the phase derivative.

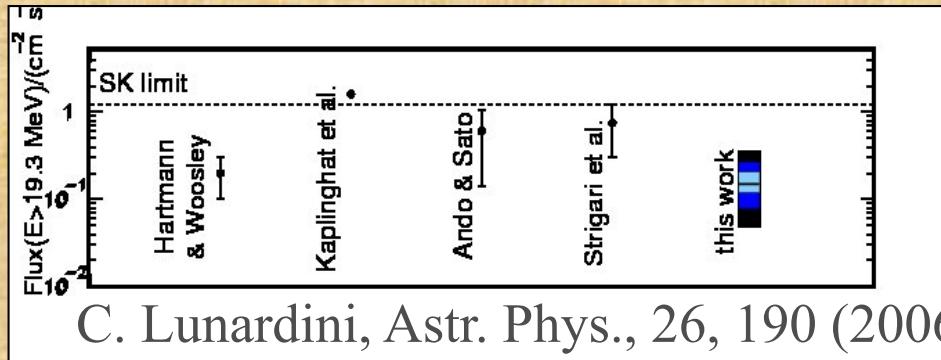
# The supernova neutrino background

Present limits :

$1.08 \bar{\nu}_e \text{ cm}^{-2} \text{s}^{-1}$  from SK ( $E_{\nu_e} > 19.3 \text{ MeV}$ ) Malek et al, PRL 90 (2003) & 2009  
 $6.8 \cdot 10^3 \nu_e \text{ cm}^{-2} \text{s}^{-1}$  from LSD ( $25 < E_{\nu_e} < 50 \text{ MeV}$ ) Aglietta et al. A Phys 1 (1992)



Yuksel, et al Astrophys. J. 683, L5(2008).



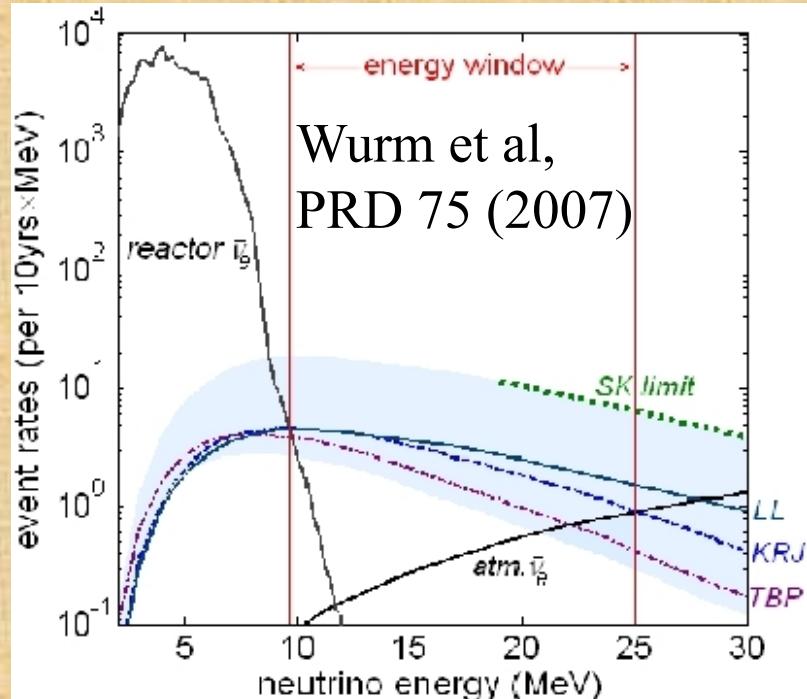
C. Lunardini, Astr. Phys., 26, 190 (2006)

## The star formation rate

The star formation rate is nowadays constrained by various observations. Uncertainties remains, especially at small redshifts (a factor of 2 at  $z = 0$ ).

Theoretical predictions on the relic neutrino fluxes are very close to the present upper limit.

# DSNB event rates in $\nu$ -observatories



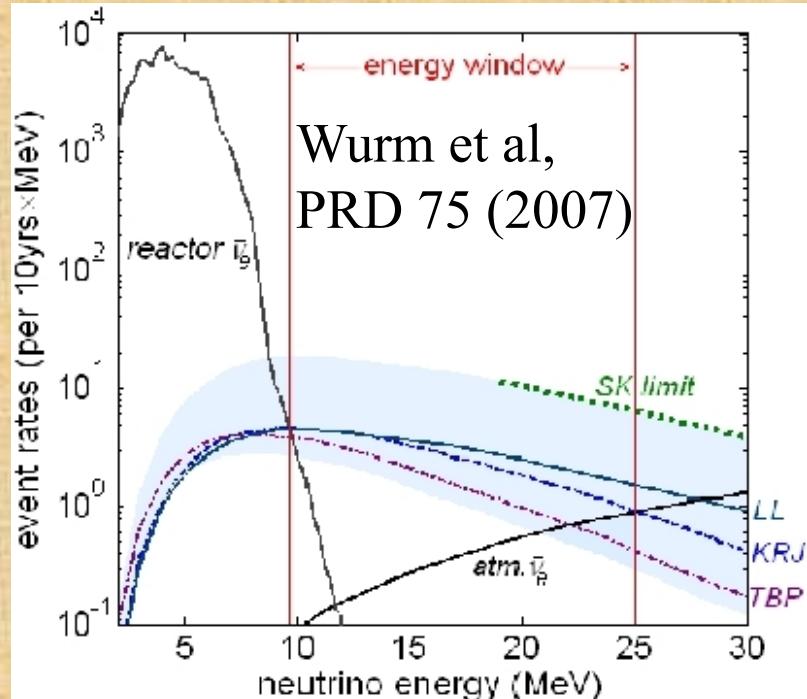
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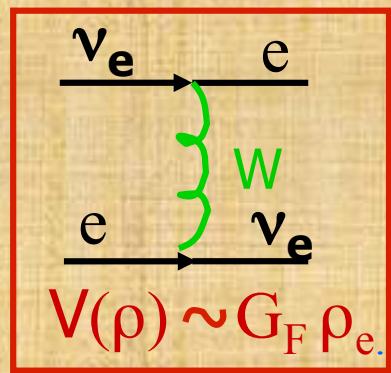
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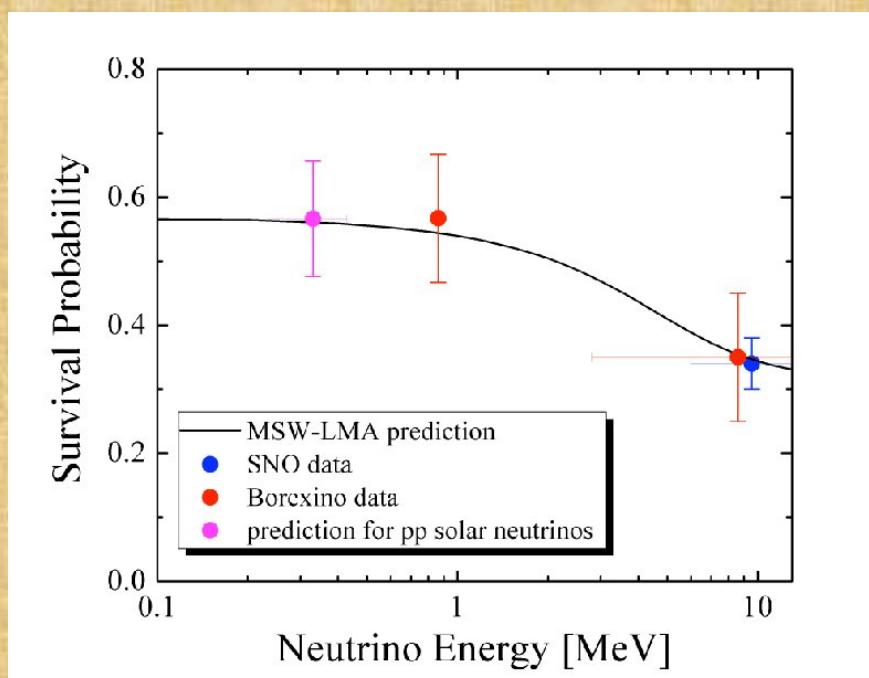
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# The Mikheev-Smirnov-Wolfenstein effect



The Mikheev-Smirnov-Wolfenstein (MSW) effect ('78, '86) : neutrino coupling with matter induces a resonant flavour conversion.



The flavour conversion depends on the adiabaticity of the propagation at the resonance (density profile and mixing parameters).

the beautiful explanation of the « solar neutrino deficit » problem !

Borexino Collaboration, J. Conf. Ser. 202, 012028 (2010)